



Lepton Flavour Universality tests at LHCb

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on behalf of the LHCb Collaboration



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Outline:

- Introduction
- LHCb detector & data taking
- $b \rightarrow c \ell \nu$
- $b \rightarrow s \ell^+ \ell^-$
- Summary

Lepton Flavour Universality

In the Standard Model (SM) quarks and leptons exist in 3 generations of 2 members each. SM assumes Lepton Flavour Universality (LFU):

- the equal gauge couplings for all 3 generations
- difference is only due to mass

LFU is established in the decay of light mesons, e.g. $\pi \rightarrow \ell\nu$, $K \rightarrow \pi\ell\ell$, $J/\psi \rightarrow \ell\ell$

LEP measurements of decays $W \rightarrow \ell\nu$ and $Z \rightarrow \ell\ell$ confirm LU, however there is some tension in $W \rightarrow \tau\nu$

Some SM extensions include particles that can cause LUV and/or LFV (e.g. LQ, Z')

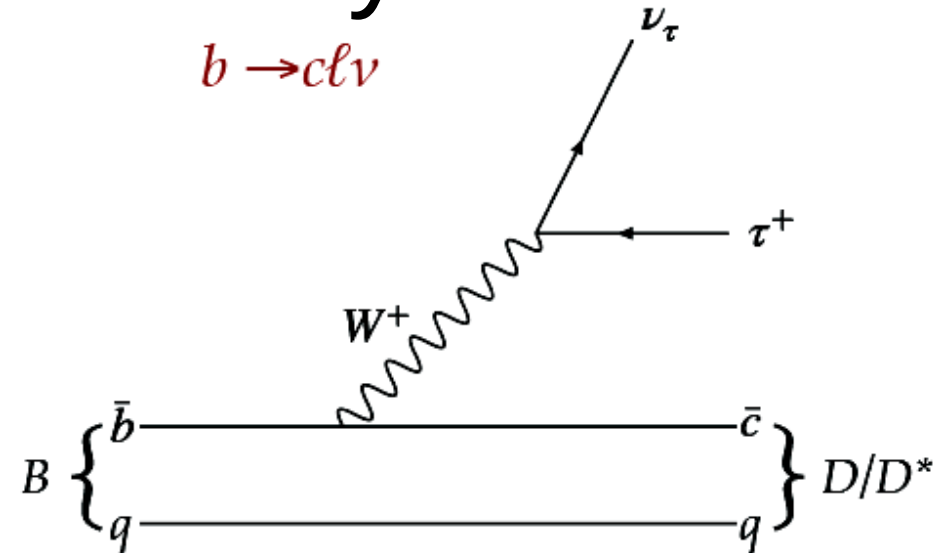
Processes with 3rd generation of quarks and leptons (B and τ) are prominent for LFU violation search:

- Lower experimental constraints
- Stronger couplings to 3rd generation predicted by BSM theories foreseeing LFU violation

LFU in b decays

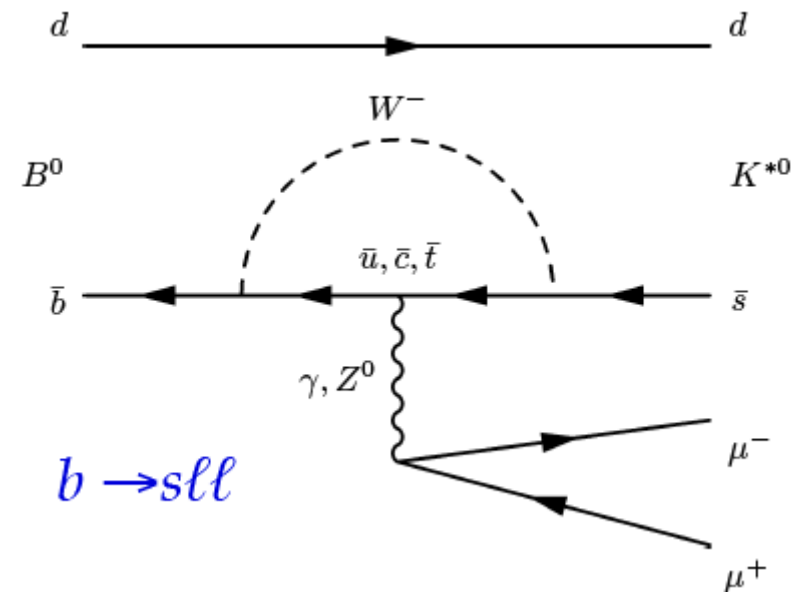
Tree-level decays $b \rightarrow c\ell\nu$

- abundant
- very well known in the SM
- BSM theories predict enhanced coupling with 3rd generation \rightarrow
 \rightarrow interested in testing τ against μ / e

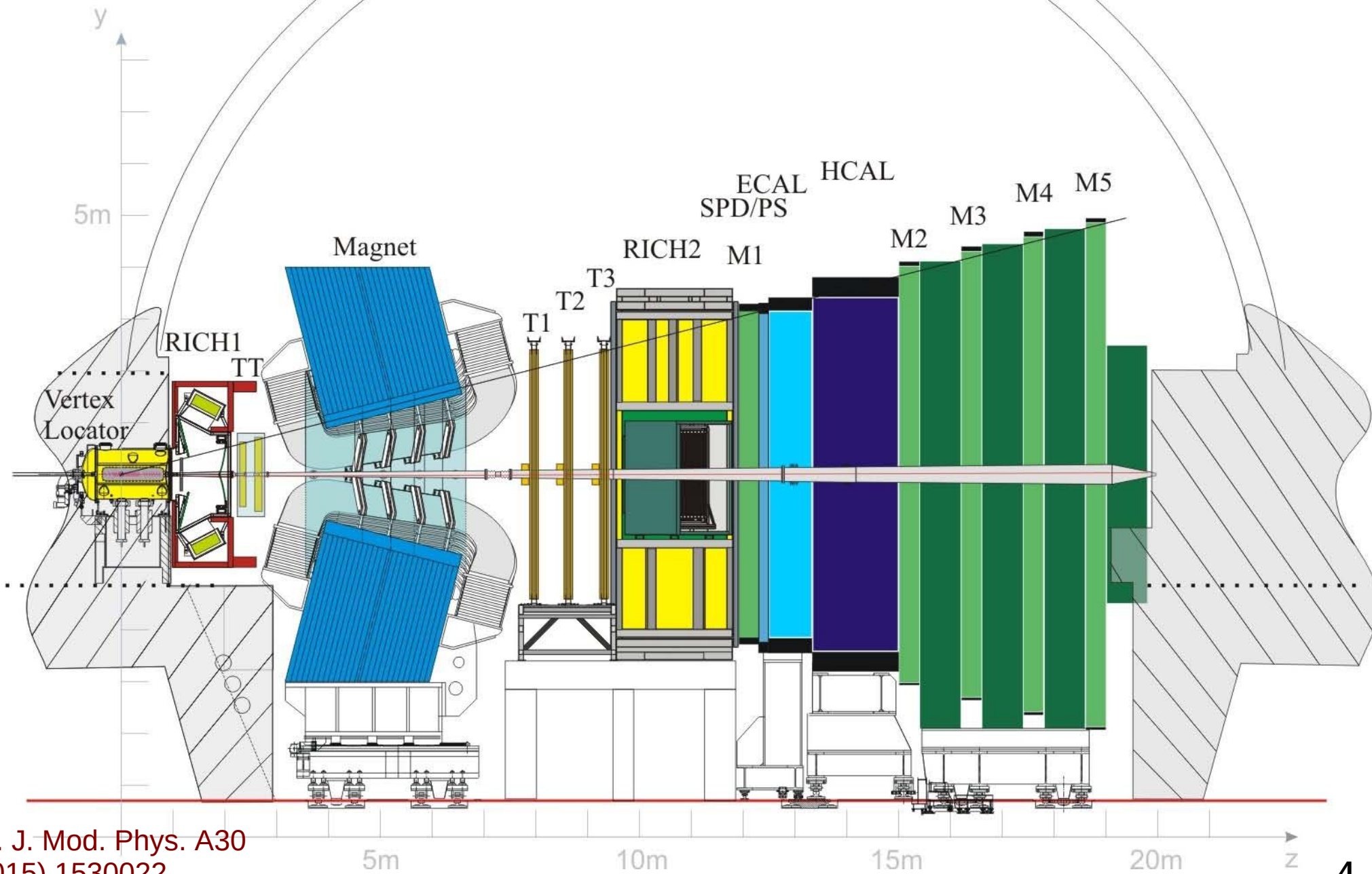


Loop-level decays $b \rightarrow s\ell^+\ell^-$

- forbidden at tree-level in SM
- sensitive to NP contributions in loops



LHCb experiment

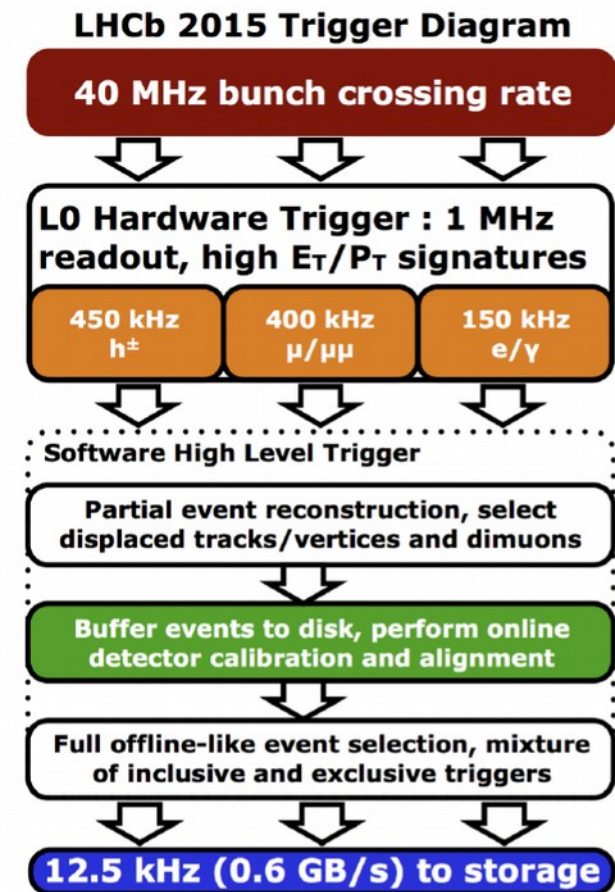
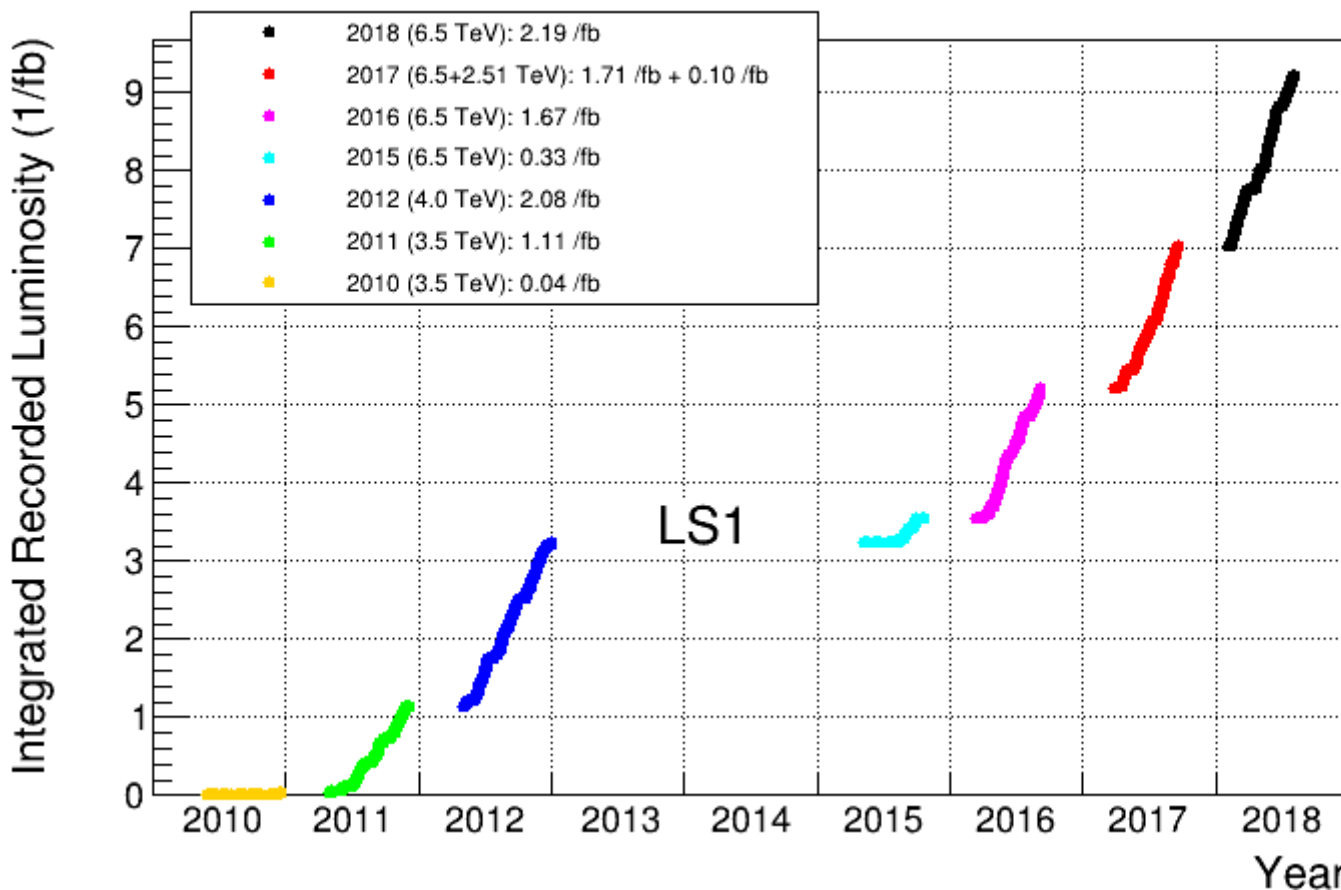


LHCb performance

Acceptance: $2 < \eta < 5$

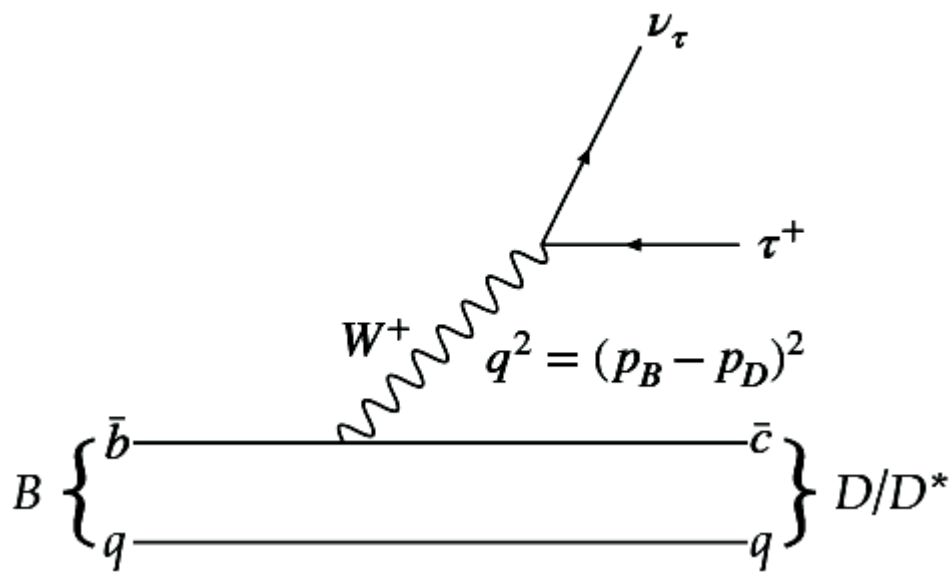
- Momentum resolution: 0.4 – 0.6% at 5 – 100 GeV
- Muon ID efficiency: 97 % with 1-3 % $\pi \rightarrow \mu$ mis-ID probability
- Electron ID efficiency: 90% with 4% $h \rightarrow e$ mis-ID probability
- Kaon ID efficiency: 95% with 5 % $\pi \rightarrow K$ mis-ID probability

LHCb Cumulative Integrated Recorded Luminosity in pp, 2010-2018



Int. J. Mod. Phys. A 30
(2015) 153022

LFU in semileptonic b decays



$$\frac{d\Gamma}{dq^2}(B \rightarrow D\ell\nu) \propto G_F^2 |V_{cb}|^2 f(q^2)^2$$

$q^2 =$ transferred momentum from the W

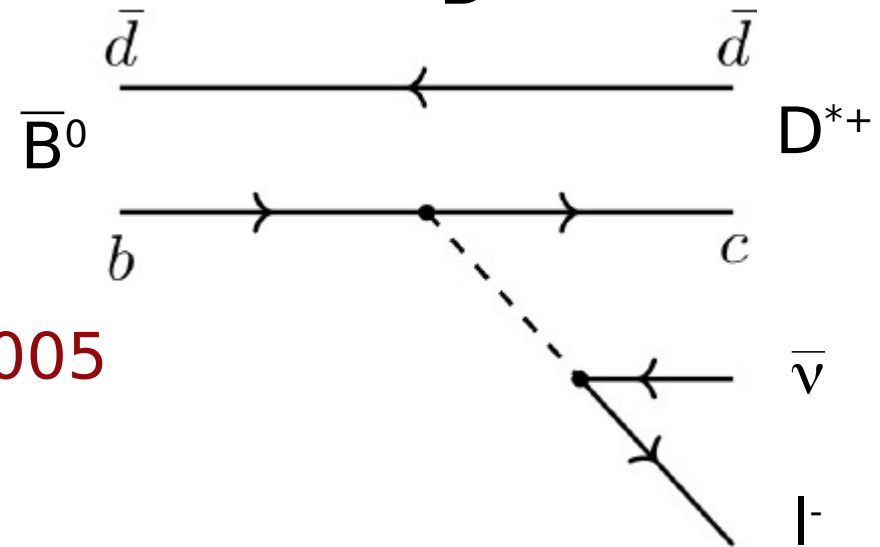
Measurement of ratios of branching fractions allows to

- cancel $|V_{cb}|$ dependence
- partially cancel out model uncertainties
- reduce experimental systematic uncertainties

SM prediction of R_{D^*}

$$R_{D^*} \equiv \frac{\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu)} \stackrel{\text{SM}}{=} 0.258 \pm 0.005$$

HFLAV average



- Hadronic uncertainties cancel to large extent in the ratio
- Difference from unity due to different lepton masses

- First deviation from SM was observed by BaBar and Belle
- LHCb performed two independent measurements using
 - $\tau^- \rightarrow \mu^- \bar{\nu}_\tau \bar{\nu}_\mu$ [PRL 115 (2015) 111803]
 - $\tau^- \rightarrow \pi^- \pi^+ \pi^- \bar{\nu}_\tau$ [PRD 97 (2018) 072013]

R_{D^*} in muonic τ decays

- τ reconstructed by $\tau^- \rightarrow \mu^- \nu_\tau \bar{\nu}_\mu$
- Both channels have the same final state ($K\pi\pi\mu$)

- Separation using three kinematic parameters:

‣ $E_\mu^* = E_\mu$ in \bar{B}^0 rest frame

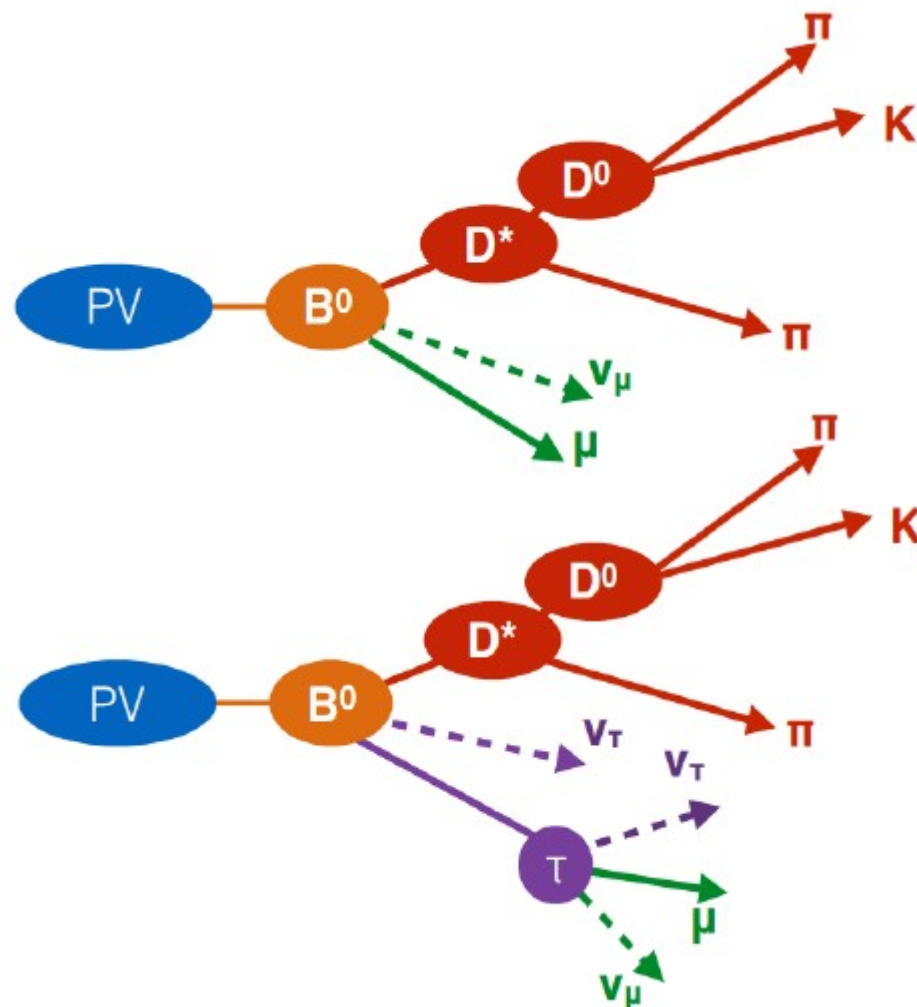
‣ $m_{\text{miss}}^2 = (p_{B^0} - p_{D^*} - p_\mu)^2$

‣ $q^2 = (p_{B^0} - p_{D^*})^2$

- Approximate p_{B^0} using

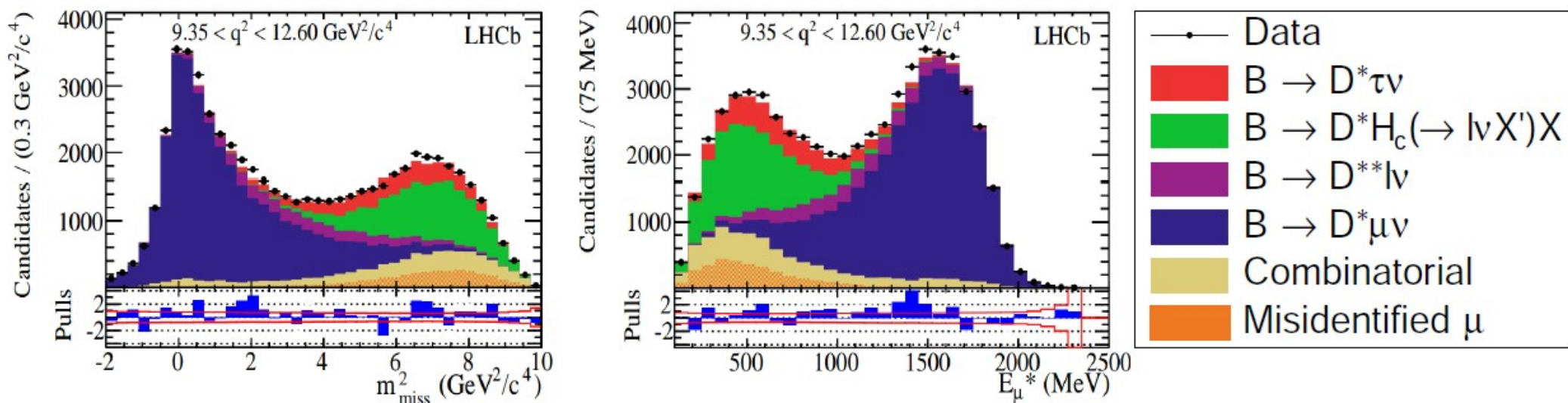
‣ \bar{B}^0 flight direction

‣ $(p_{B^0})_z = m_B/m_{\text{reco}} (p_{\text{reco}})_z$



R_{D^*} in muonic τ decays

- Yields are extracted with a 3D binned ML fit in E_μ^* , m_{miss}^2 , q^2
- Templates for the signal, normalization and backgrounds are obtained on MC and checked against control samples



- $R_{D^*} = 0.336 \pm 0.027$ (stat) ± 0.030 (syst) 2σ above SM
- Main background: Partially reconstructed and mis-ID decays
- Main systematic: Size of the simulated sample

R_{D^*} in hadronic τ decays

τ reconstructed by $\tau^- \rightarrow \pi^- \pi^- \pi^+ \nu_\tau$ independent from R_{D^*} muonic

$$R_{D^*} = \underbrace{\frac{\mathcal{B}(B^0 \rightarrow D^{*-} \tau^+ \nu_\tau)}{\mathcal{B}(B^0 \rightarrow D^{*-} 3\pi)}}_{\text{measured ratio } \mathcal{K}(D^{*-})} \cdot \underbrace{\frac{\mathcal{B}(B^0 \rightarrow D^{*-} 3\pi)}{\mathcal{B}(B^0 \rightarrow D^{*-} \mu^+ \nu_\mu)}}_{\text{external inputs}}$$

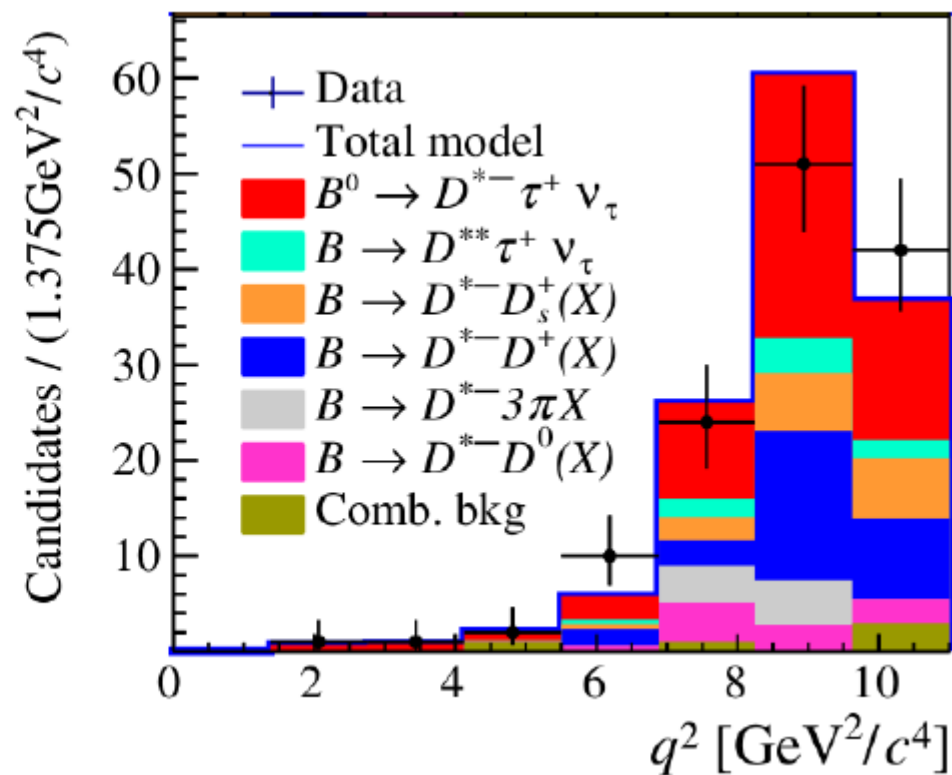
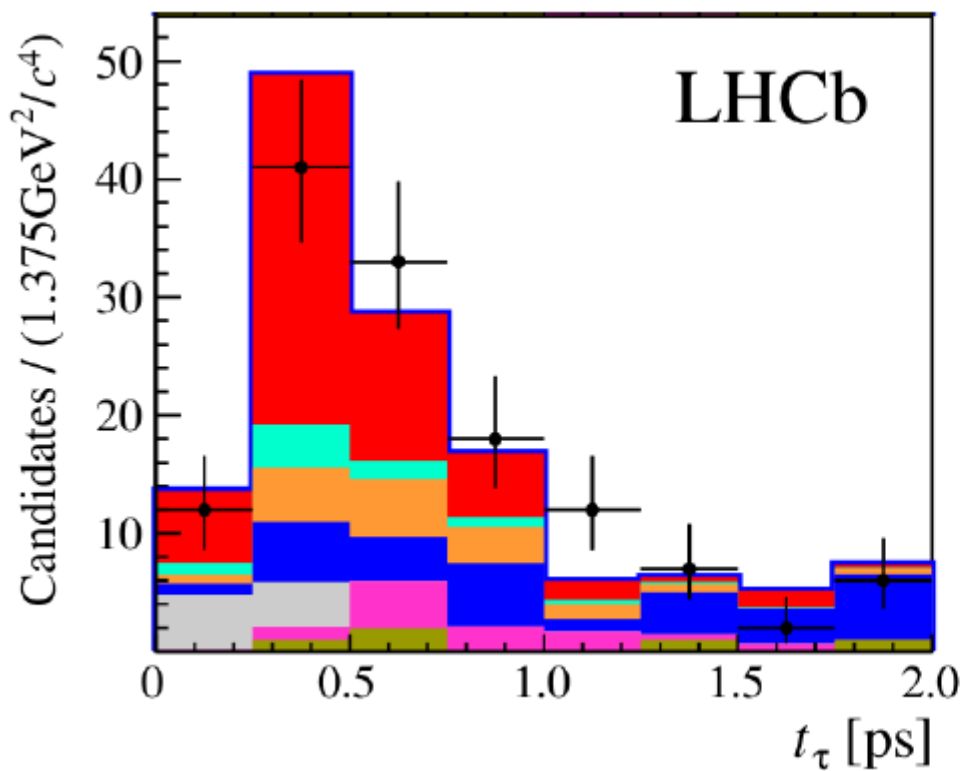
~4% precision
(BABAR, Belle, LHCb)

~2% precision, HFLAV

- Partial cancellation of experimental systematic uncertainties
- Main background:
 - $B^0 \rightarrow D^* \pi \pi \pi X$, suppressed with τ decay time, t_τ
 - $B \rightarrow DD_{(s)} X$, suppressed with BDT

R_{D^*} in hadronic τ decays

Yields are extracted by a binned ML fit on q^2 , BDT and t_τ

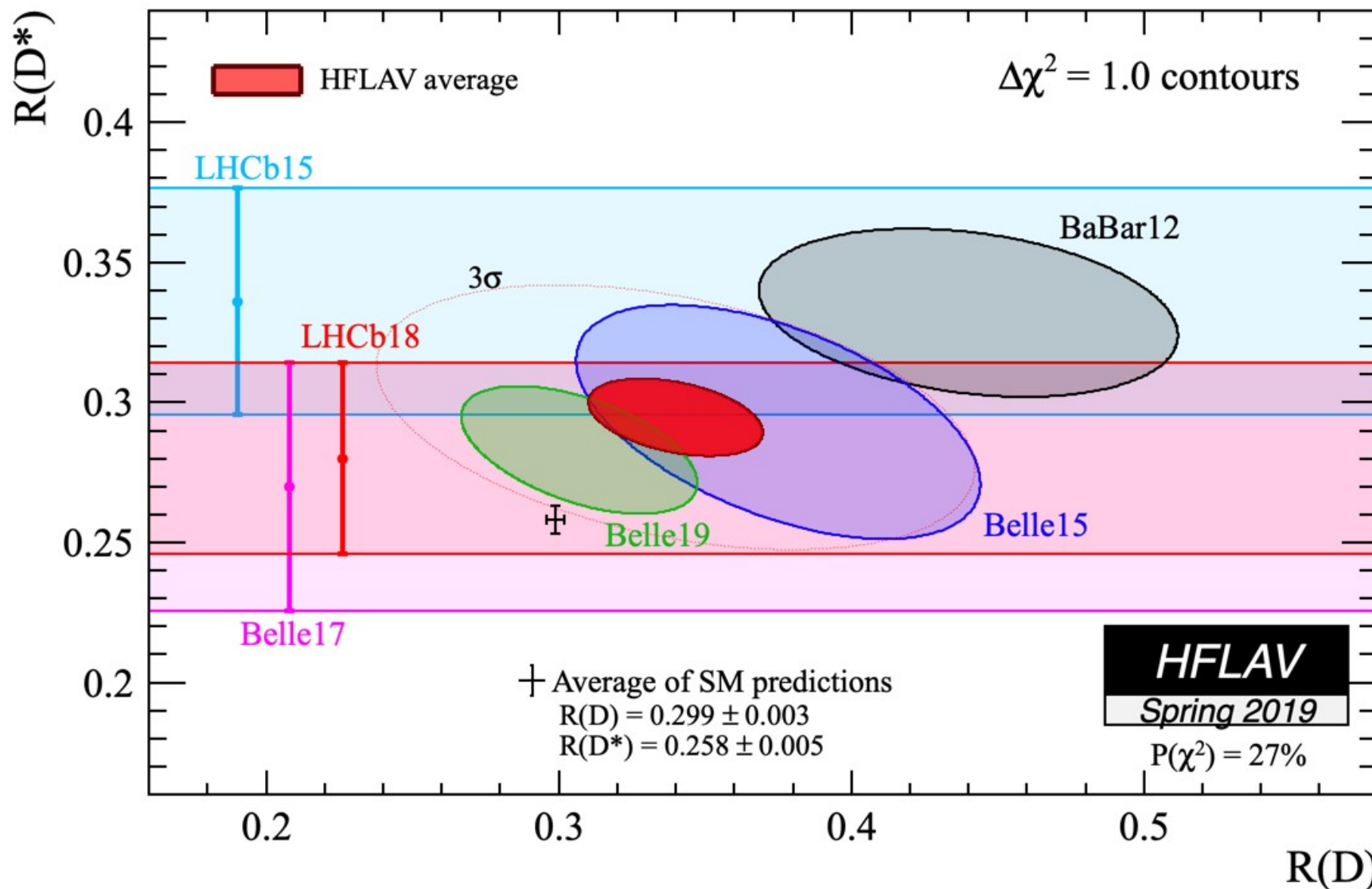


- $R_{D^*} = 0.291 \pm 0.019$ (stat) ± 0.026 (syst) ± 0.013 (ext)

1 σ above SM

- Main systematic: Size of the simulated sample

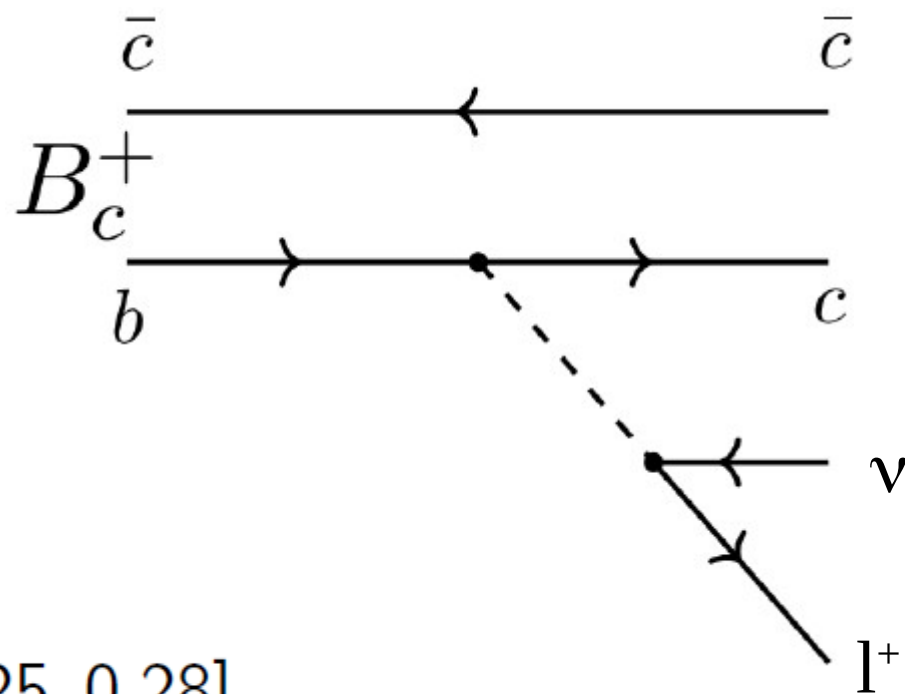
R_{D^*} results



- LHCb average: $R_{D^*} = 0.310 \pm 0.016 \pm 0.022$ 2.2σ above SM
- Measurements of R_D and R_{D^*} are consistent with each other
- Combined result is 3.1σ above SM prediction

SM prediction of $R_{J/\psi}$

Test of LFU in $b \rightarrow c \ell \nu$ decays
 with a different spectator quark
 using large B_c^+ sample available
 at LHCb



$$R_{J/\psi} \equiv \frac{\mathcal{B}(B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau)}{\mathcal{B}(B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu)} \stackrel{\text{SM}}{\in} [0.25, 0.28]$$

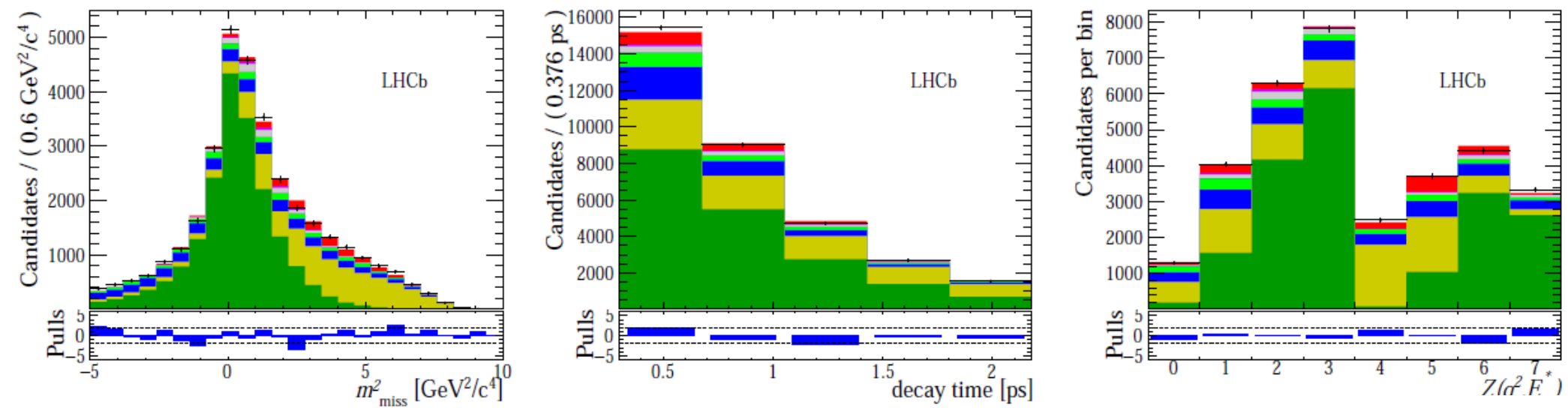
Interval is due to form factor uncertainty [PLB 452 (1999) 129]
 [arXiv:hep-ph/0211021] [PRD 73 (2006) 054024] [PRD 74 (2006) 074008]

Lattice calculation is in progress

$R_{J/\psi}$ results

τ reconstructed by $\tau^- \rightarrow \mu^- \nu_\tau \bar{\nu}_\mu$

Analysis strategy as in $R_{D^*} + t_\tau$ as 4th discriminating variable



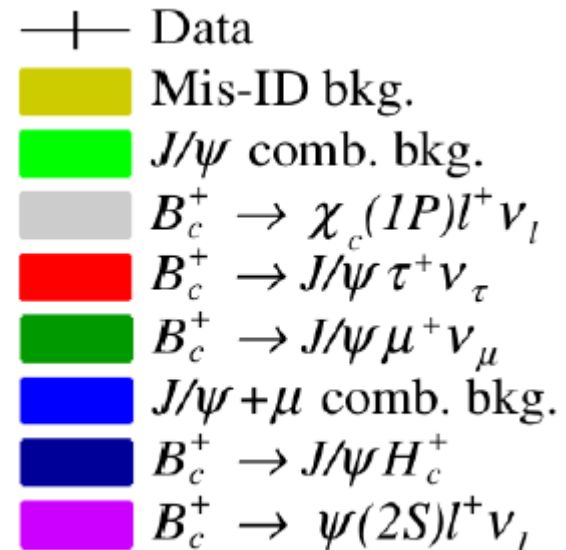
Main backgrounds: $B \rightarrow J/\psi + \text{mis-ID hadron}$
 Systematic: MC sample, $B_c^+ \rightarrow J/\psi$ form factors

$$R_{J/\psi} = 0.71 \pm 0.17(\text{stat}) \pm 0.18(\text{syst})$$

Phys.Rev.Lett. 120 121801 (2018)

First evidence (3σ) of $B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau$

Run1: 3.0 fb⁻¹



LFU tests in $b \rightarrow s \ell \ell$

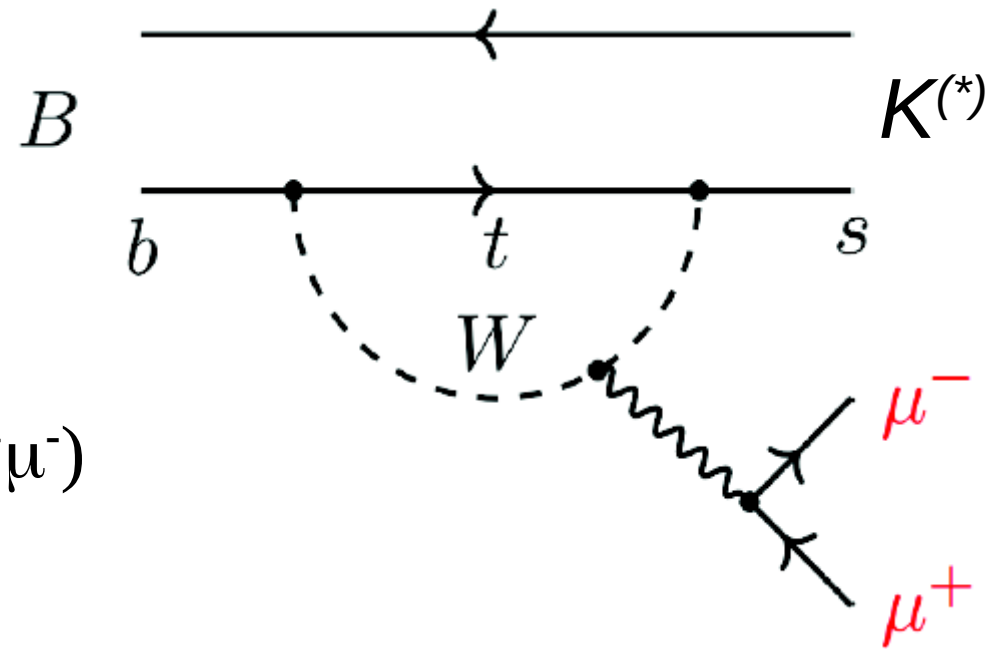
$b \rightarrow s \ell^+ \ell^-$ are FCNC processes that can only occur at loop-level in SM

Measure $R_{K^{(*)}}$ in bins of $q^2 \equiv m^2(\mu^+ \mu^-)$

$$R_K \equiv \frac{\mathcal{B}(B \rightarrow K \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K e^+ e^-)} \stackrel{\text{SM}}{=} 1 \pm \underbrace{\mathcal{O}(10^{-3})}_{\text{neglect } m_\ell} \pm \underbrace{\mathcal{O}(10^{-2})}_{\text{QED effects}} \quad [\text{EPJC76(2016)8,440}]$$

Use double ratio to reduce systematic effects:

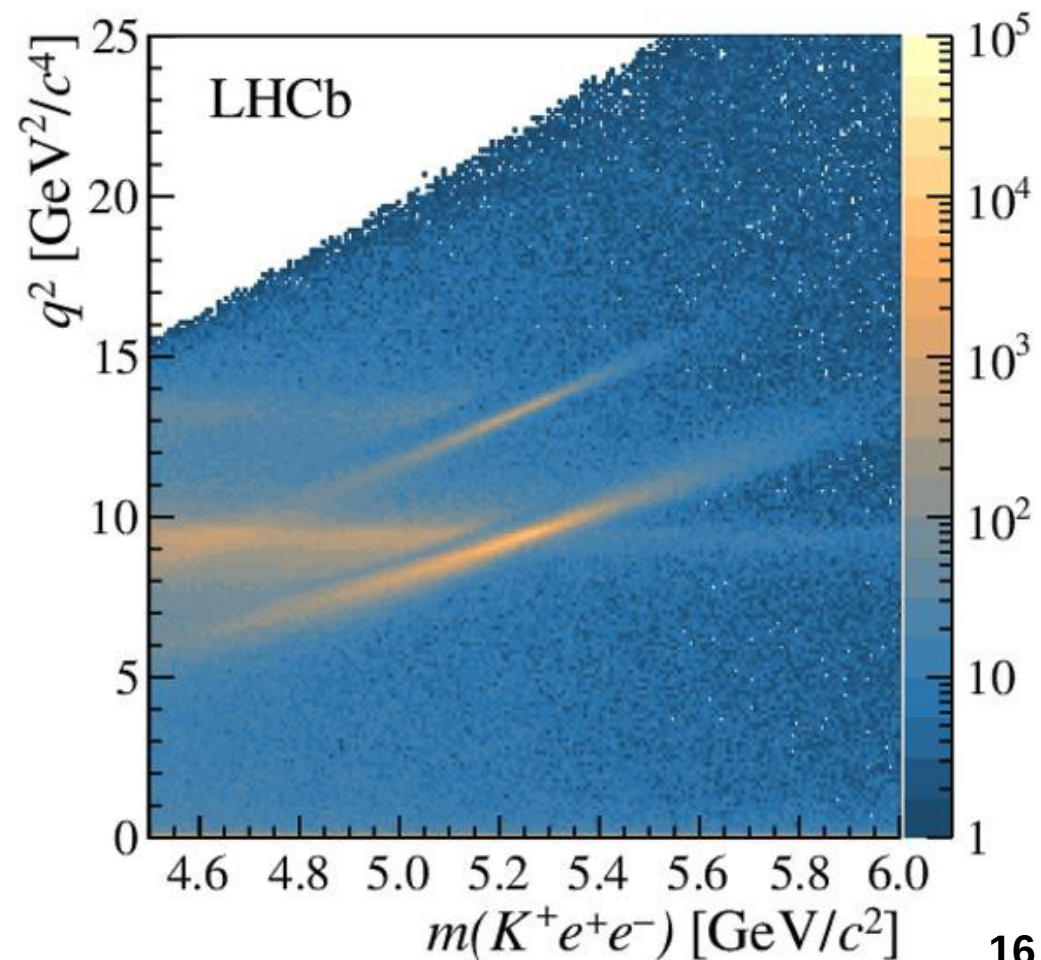
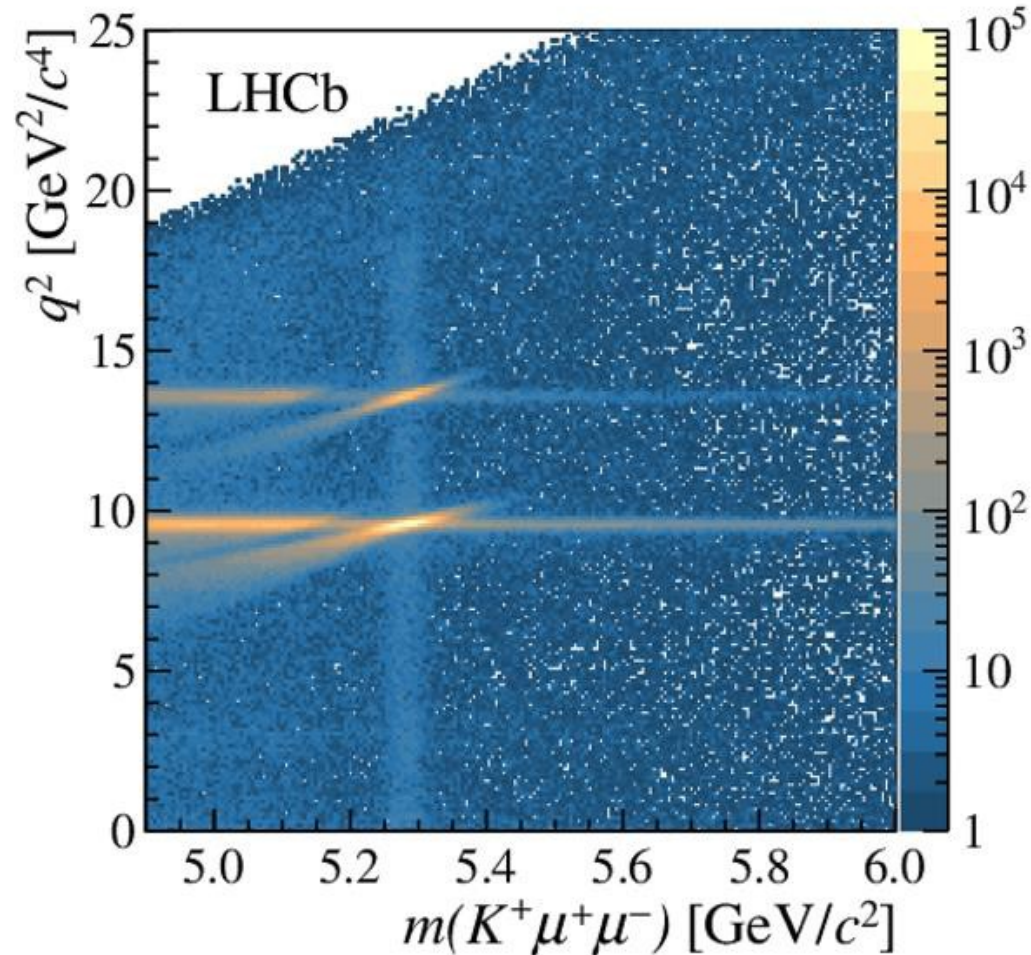
$$R_{K^{(*)}} \equiv \frac{\mathcal{B}(B \rightarrow K \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K (J/\psi \rightarrow \mu^+ \mu^-))} \cdot \frac{\mathcal{B}(B \rightarrow K (J/\psi \rightarrow e^+ e^-))}{\mathcal{B}(B \rightarrow K e^+ e^-)}$$



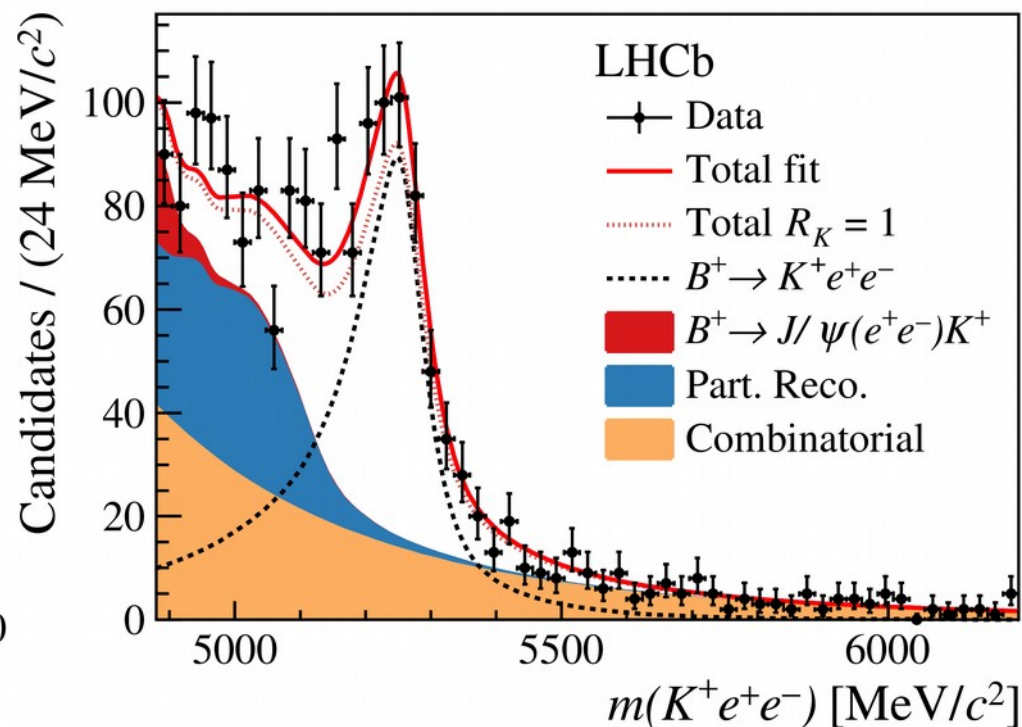
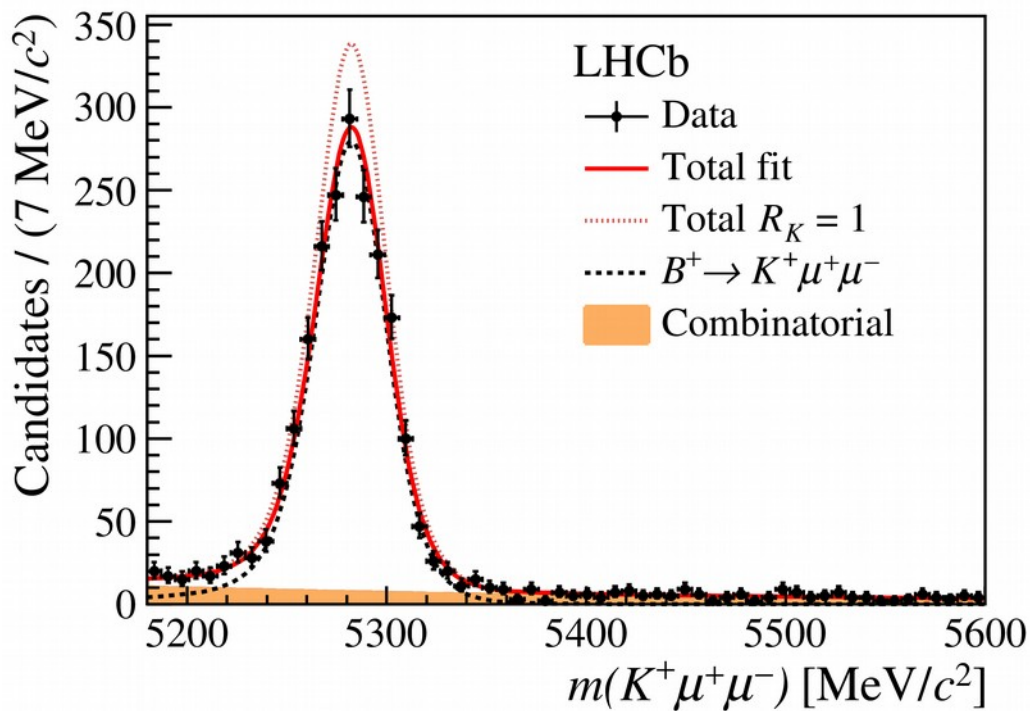
R_K measurement

Phys. Rev. Lett. 122 (2019) 191801

- Combination of K^+ with 2 opposite-sign leptons
- Bremsstrahlung correction for electrons
- Veto $b \rightarrow c$ by requiring $m(K^+ l^-) > m(D^0)$
- Selection using Boosted Decision Tree with 13 kinematical variables



R_K fit results

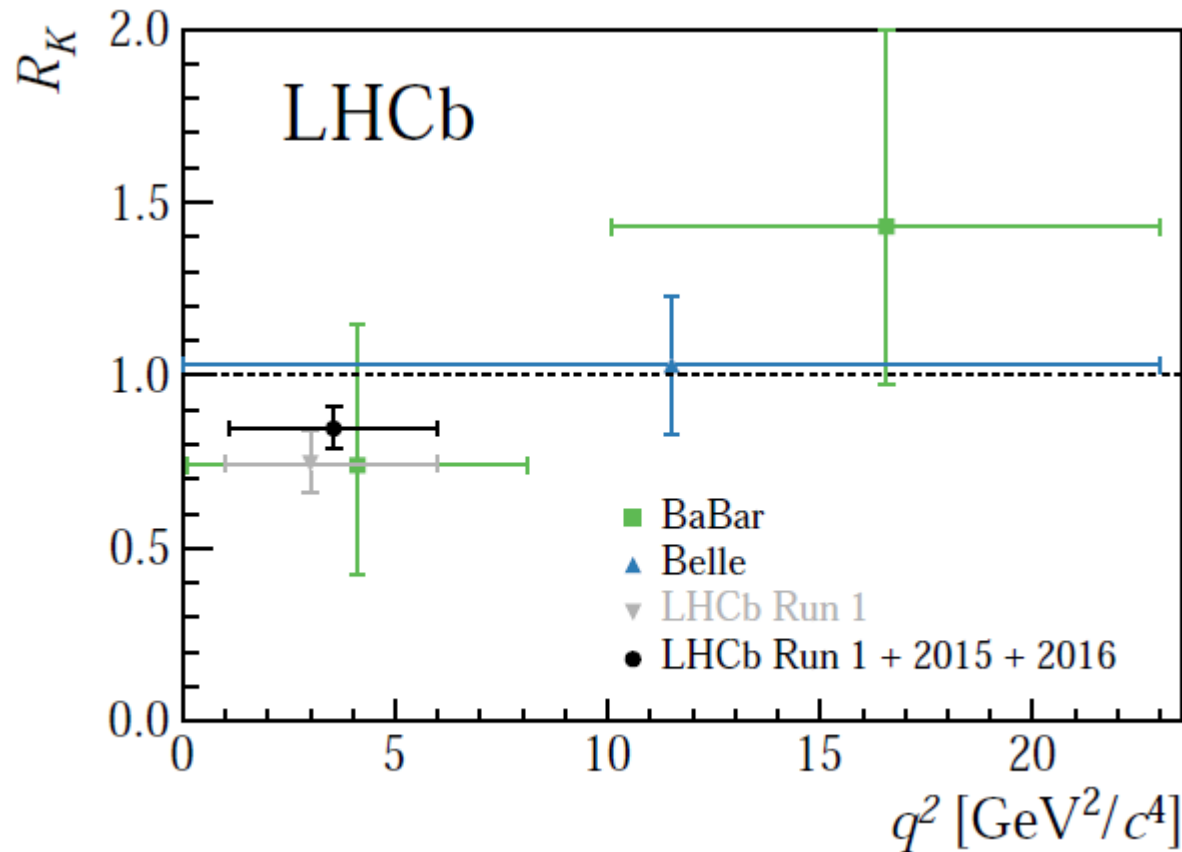


Decay Mode	Event Yield	
$B^+ \rightarrow K^+ e^+ e^-$	766 ± 48	
$B^+ \rightarrow K^+ \mu^+ \mu^-$	$1\,943 \pm 49$	
$B^+ \rightarrow J/\psi(\rightarrow e^+ e^-) K^+$	$344\,100 \pm 610$	
$B^+ \rightarrow J/\psi(\rightarrow \mu^+ \mu^-) K^+$	$1\,161\,800 \pm 1\,100$	

Simultaneous unbinned maximum likelihood fits:

- Signal: Gaussian core with power-law tails
- Combinatorial background: exponential
- Partially reconstructed background from simulated $B \rightarrow K^* l^+ l^-$

R_K result



Using 2011 and 2012 LHCb data, R_K was:

$$R_K = 0.745_{-0.074}^{+0.090}(\text{stat.}) \pm 0.036(\text{syst.}),$$

$\sim 2.6 \sigma$ from SM ([PRL113\(2014\)151601](#)).

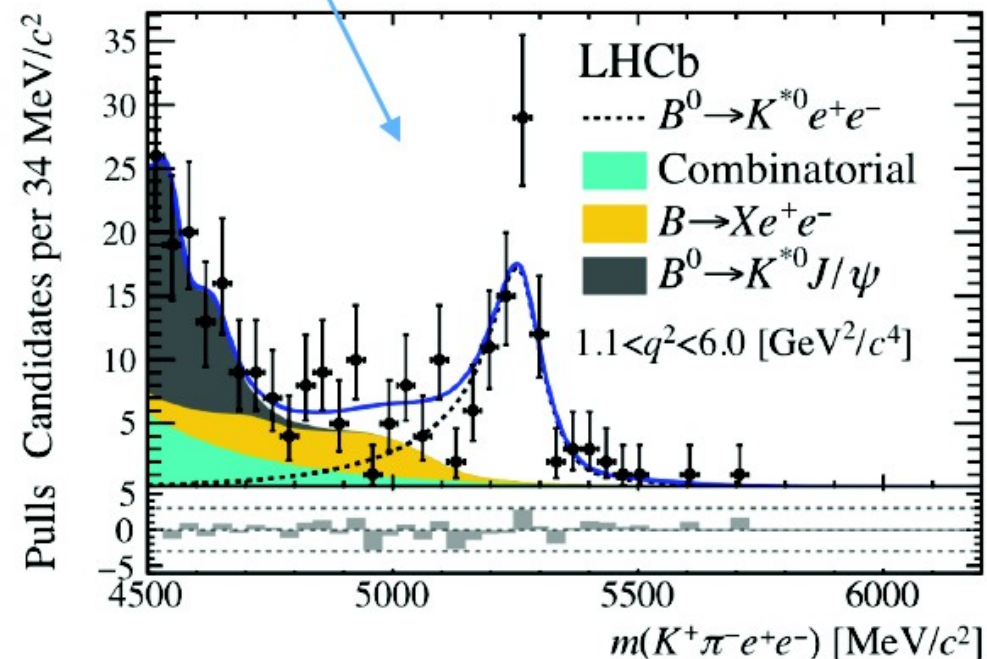
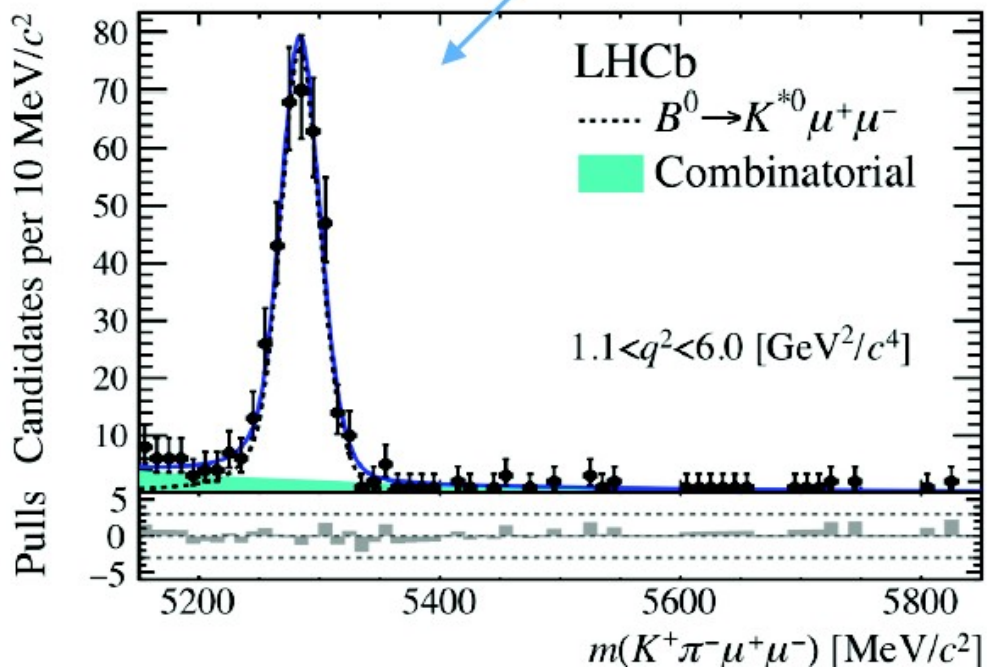
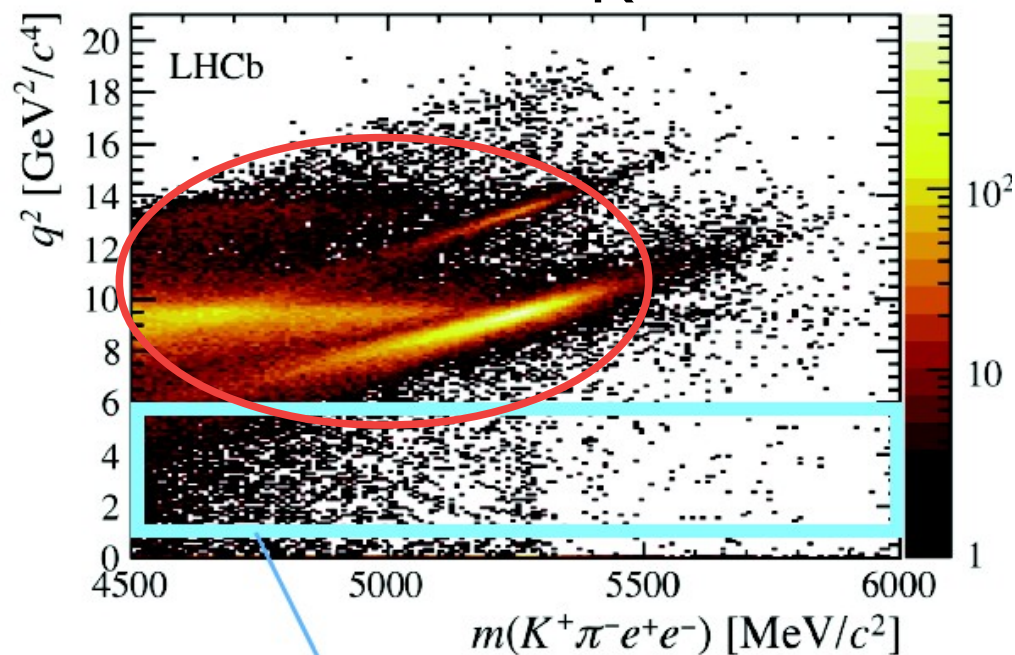
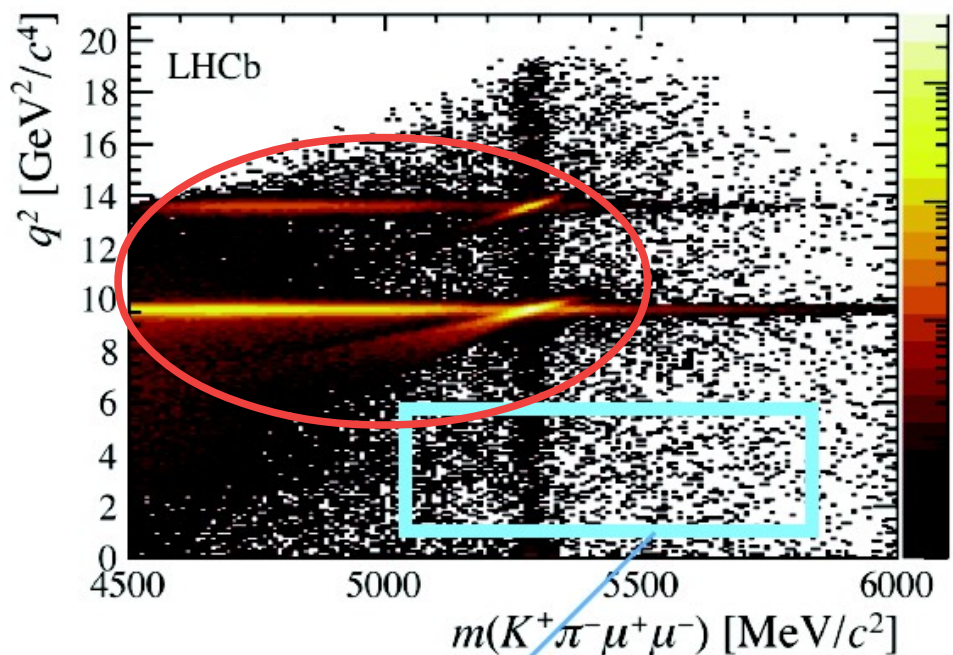
$$R_K = 0.846_{-0.054}^{+0.060}(\text{stat.})_{-0.014}^{+0.016}(\text{syst.})$$

$\sim 2.5 \sigma$ from SM.

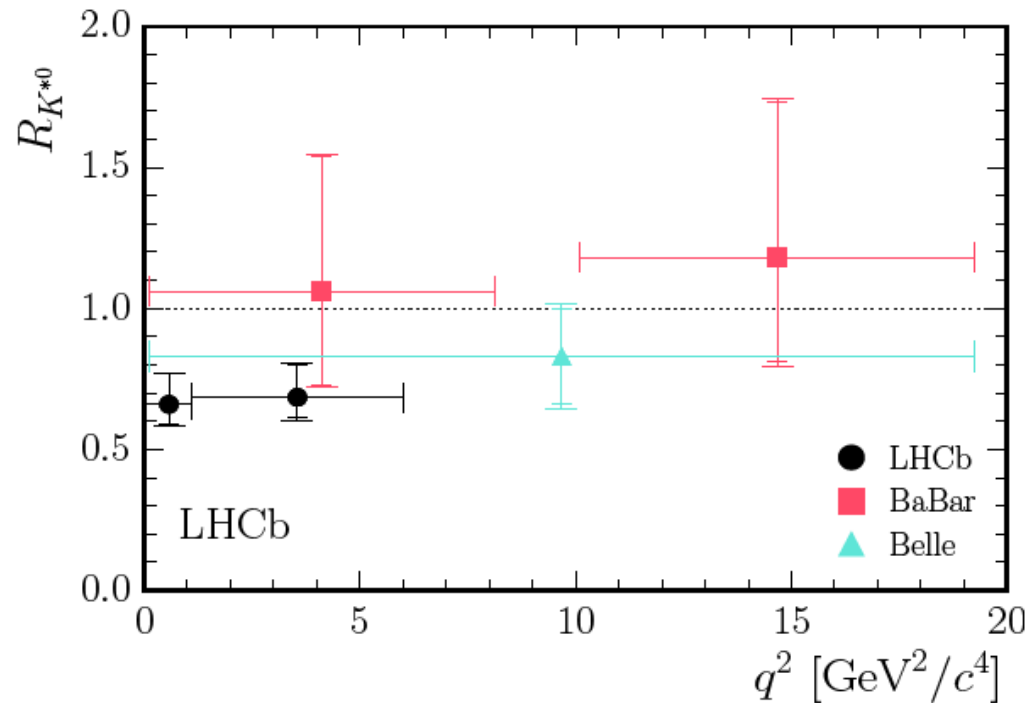
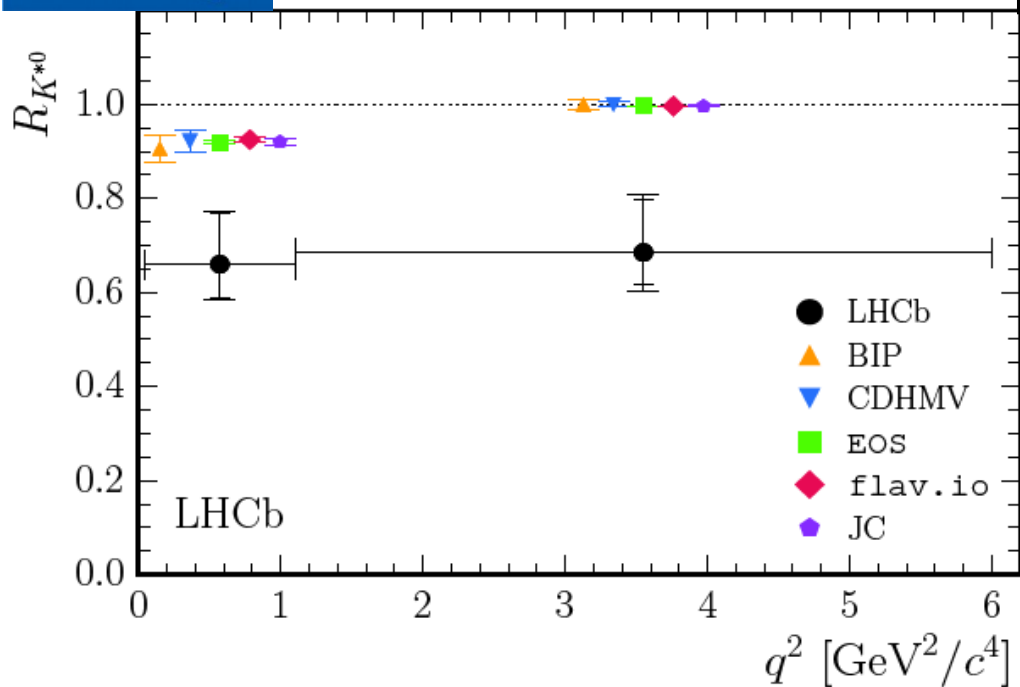
Dominant systematic uncertainties:

Fit shape, trigger calibration, B^+ kinematics.

Measurement of R_{K^*}



R_{K^*} results



$$R_{K^*} = \begin{cases} 0.66^{+0.11}_{-0.07}(\text{stat}) \pm 0.03(\text{syst}), \\ 0.69^{+0.11}_{-0.07}(\text{stat}) \pm 0.05(\text{syst}), \end{cases}$$

at low q^2 ($\sim 2.2\sigma$ below SM)

at central q^2 ($\sim 2.4\sigma$ below SM)

- Most precise measurement to date
- Compatible with BaBar and Belle
- Statistically limited by the electron sample

- ▲ BIP [EPJC 76 (2016) 440]
- ▼ CDHMV [JHEP 04 (2017) 016]
- EOS [PRD 95 (2017) 035029]
- ◆ flav.io [EPJC 77 (2017) 377]
- ◆ JC [PRD 93 (2016) 014028]
- BaBar [PRD 86 (2012) 032012]
- ▲ Belle [PRL 103 (2009) 171801]

Prospects for LFU tests at LHCb

LHCb aims to perform complementary LFU tests:

- $b \rightarrow c\ell\nu$ transitions:

- $R_{\Lambda c^{(*)}}$, $R_{D^{(*)}}$, $R_{D_s^{(*)}}$ and others

- $b \rightarrow u\ell\nu$ transitions:

- $R_{pp}^- = B(B^+ \rightarrow p\bar{p}\tau^+ \nu) / B(B^+ \rightarrow p\bar{p}\mu^+ \nu)$ and others

- $b \rightarrow s\ell\ell$ transitions:

- R_{K_S} , $R_{K^{*+}}$, $R_{K_{\pi\pi}}$, R_{pK} , R_ϕ , R_Λ , direct fit to $\Delta C_9^{\mu,e}$ and others

⇒ Update of $R_{K^{*+}}$, $R_{D^{*+}}$ and $R_{J/\psi}$ with Run 2 data is currently on-going. Expected improvement on both statistical and systematic uncertainties.

Conclusion

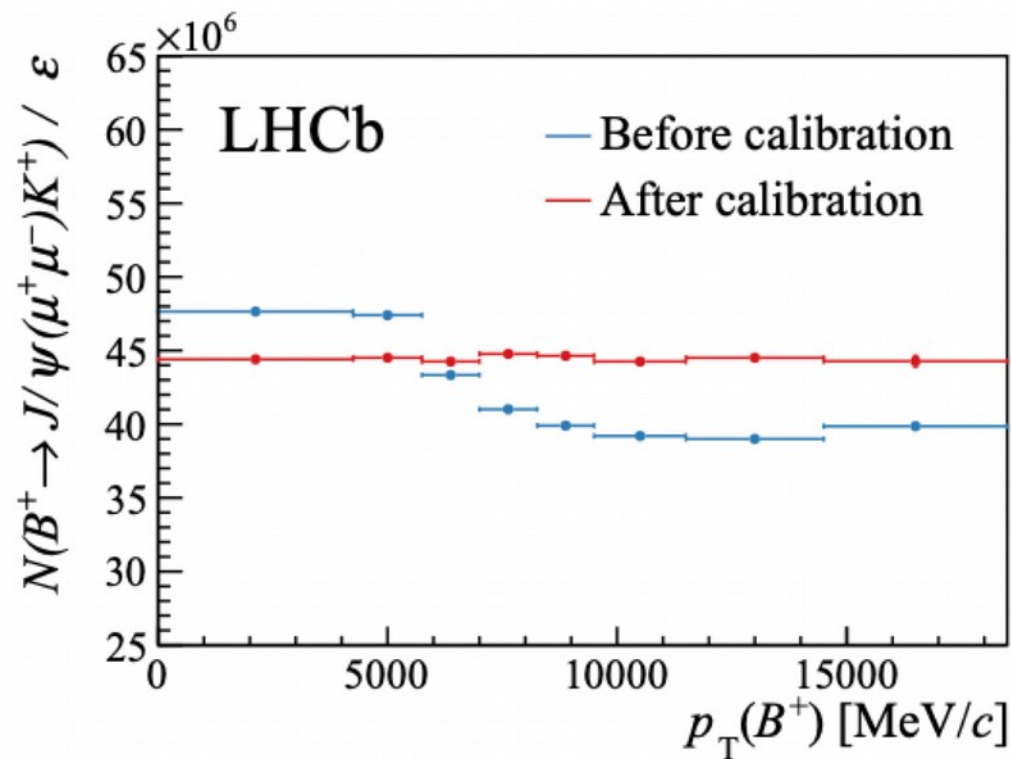
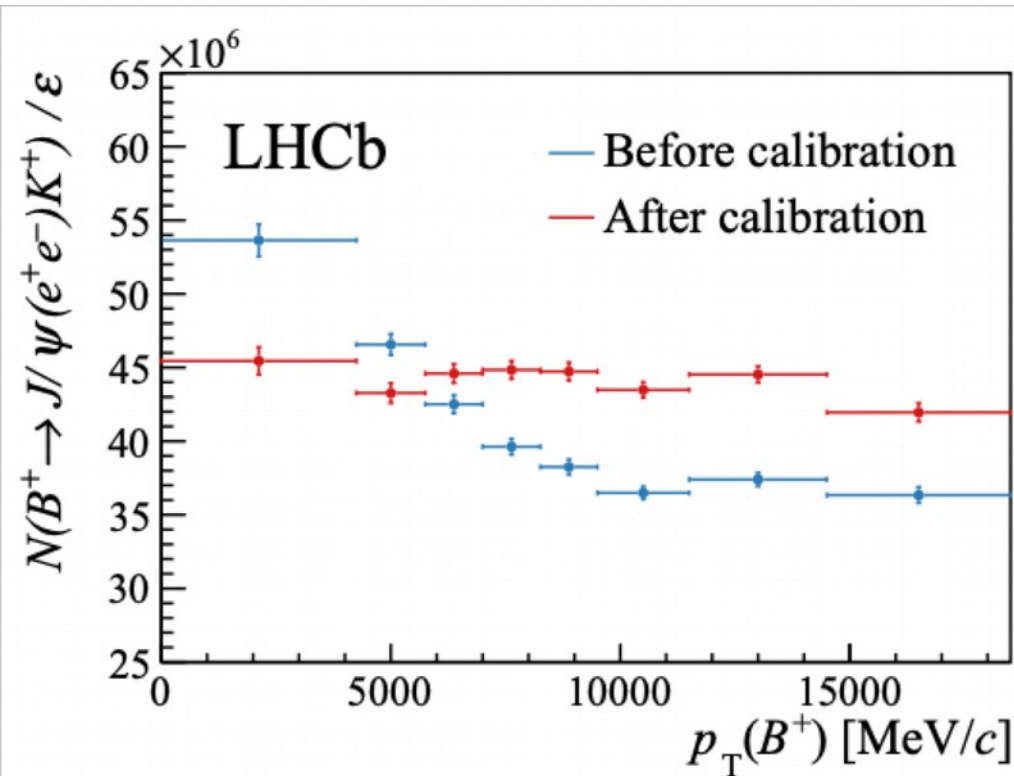
- Tests of LFU in heavy flavour physics present a tension with the SM predictions on ratios of branching fractions in both $b \rightarrow c\ell\nu$ and $b \rightarrow s\ell^+\ell^-$
 - 3.1σ tension in R_D and R_{D^*} when combining BaBar, Belle and LHCb
 - 2.5σ below SM prediction in $R_{K^{(*)}}$ at central q^2
- Anomalies in both $b \rightarrow c\ell\nu$ and $b \rightarrow s\ell^+\ell^-$ decays could be described with same New Physics models.
- Looking forward for contribution from theory community.
- LHCb continue testing the LFU hypothesis. Please stay tuned!



Backup

Efficiencies and corrections

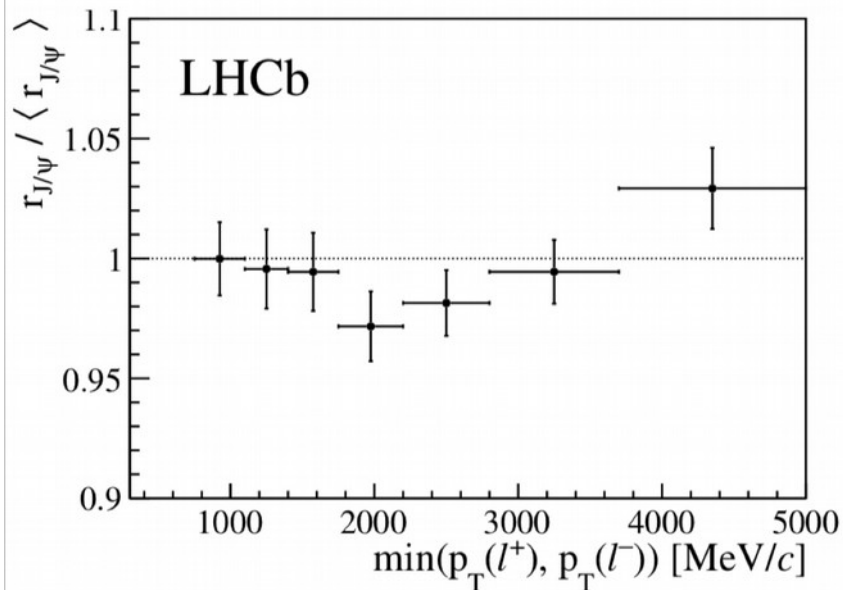
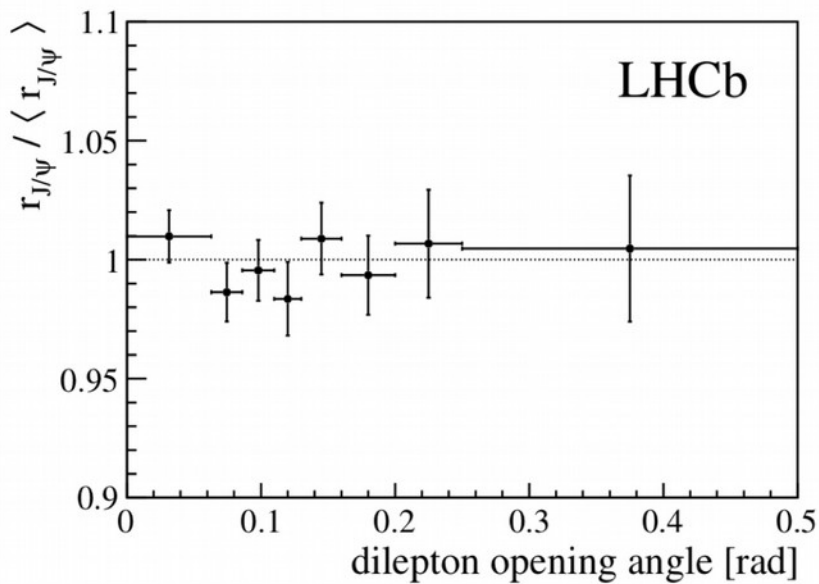
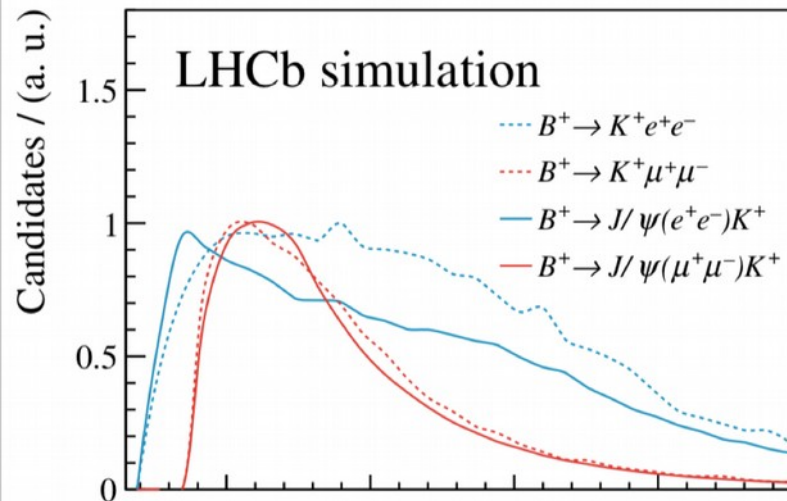
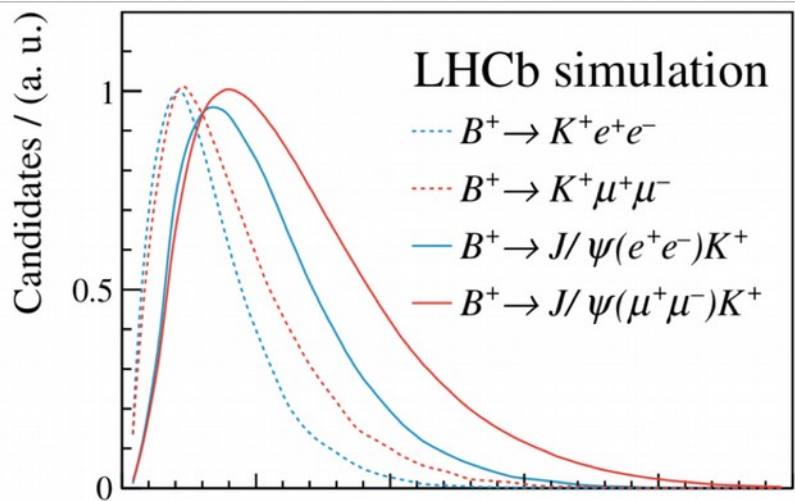
- Efficiencies calculated from simulation corrected with data:
- B^+ kinematics corrected with $B^+ \rightarrow J/\psi[\mu^+\mu^-] K^+$
- Trigger efficiency corrected with tag-and-probe $B^+ \rightarrow J/\psi[\ell^+\ell^-] K^+$
- Particle identification calibrated with data [EPJ TI (2019)6:1]
- q^2 resolution corrected based on $m(\ell^+\ell^-)$ of the J/ψ peak



Overall effect of corrections on $R_K \sim 0.02$

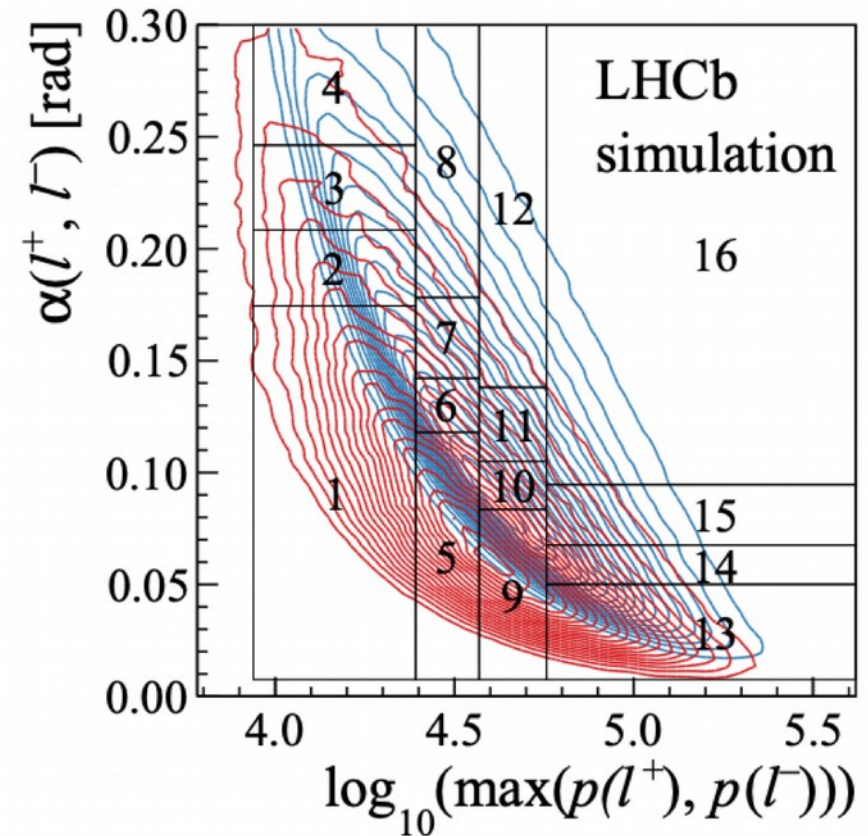
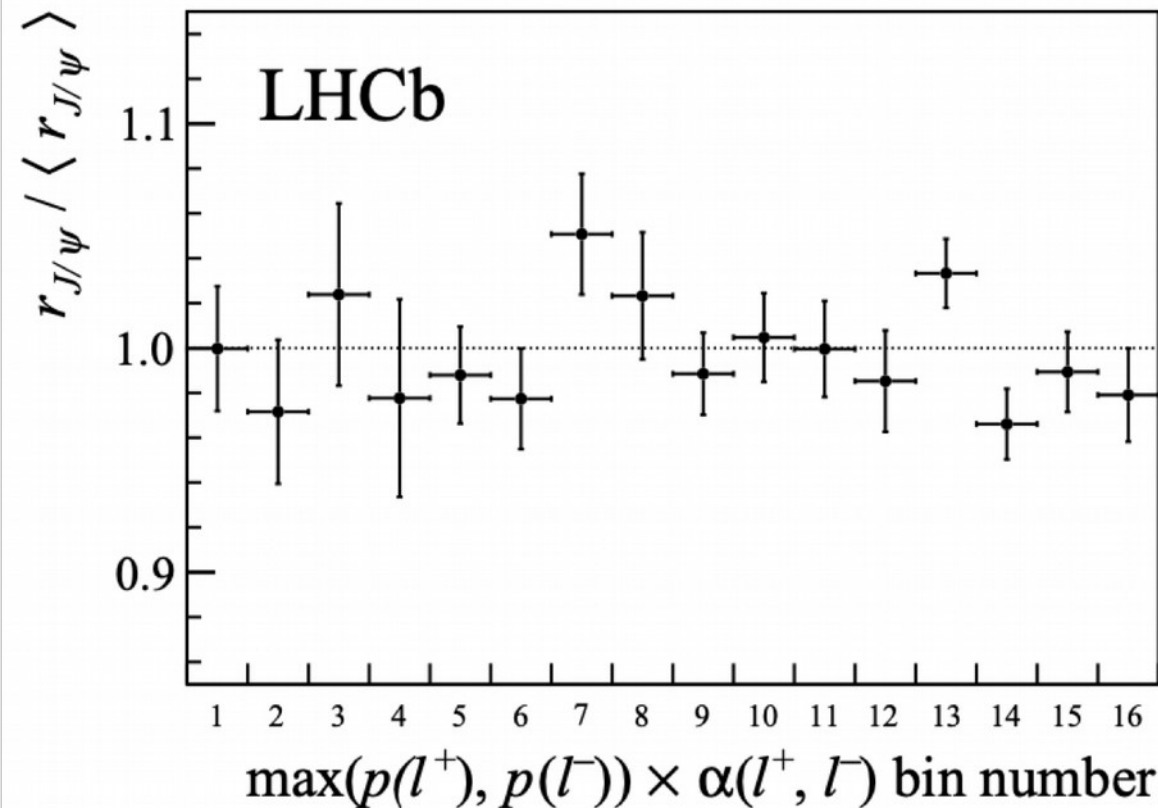
Cross checks

$$r_{J/\psi} = \frac{\mathcal{B}(B^+ \rightarrow J/\psi(\rightarrow \mu^+ \mu^-) K^+)}{\mathcal{B}(B^+ \rightarrow J/\psi(\rightarrow e^+ e^-) K^+)} = 1.014 \pm 0.035 \text{ (stat + syst)}$$



Cross checks

Dependence of $R_{J/\psi}$ on kinematical variables (2D)



Double ratio of Branching fractions:

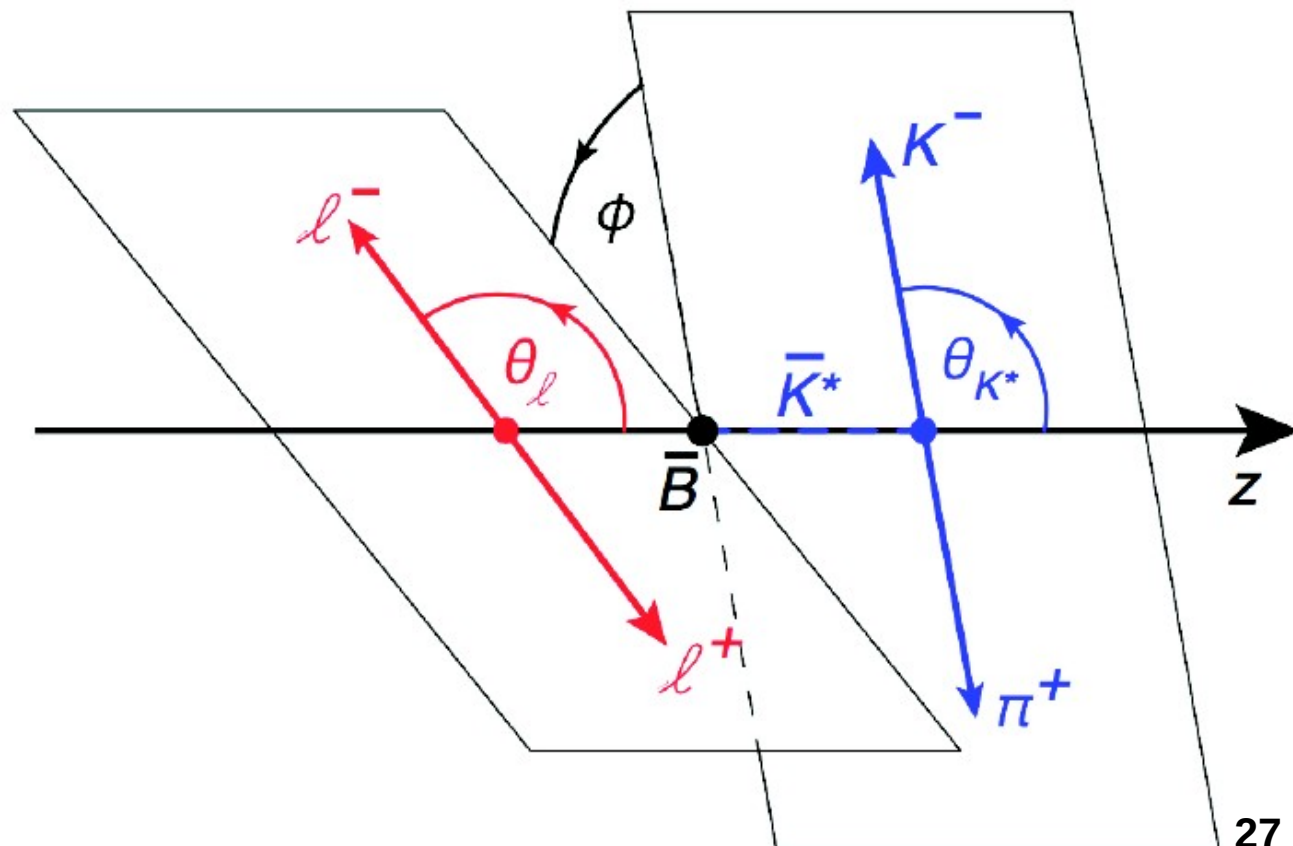
$$R_{\psi(2S)} = \frac{\mathcal{B}(B^+ \rightarrow \psi(2S)(\rightarrow \mu^+ \mu^-)K^+)}{\mathcal{B}(B^+ \rightarrow J/\psi(\rightarrow \mu^+ \mu^-)K^+)} / \frac{\mathcal{B}(B^+ \rightarrow \psi(2S)(\rightarrow e^+ e^-)K^+)}{\mathcal{B}(B^+ \rightarrow J/\psi(\rightarrow e^+ e^-)K^+)} = 0.996 \pm 0.013$$

(stat+syst)

Angular analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

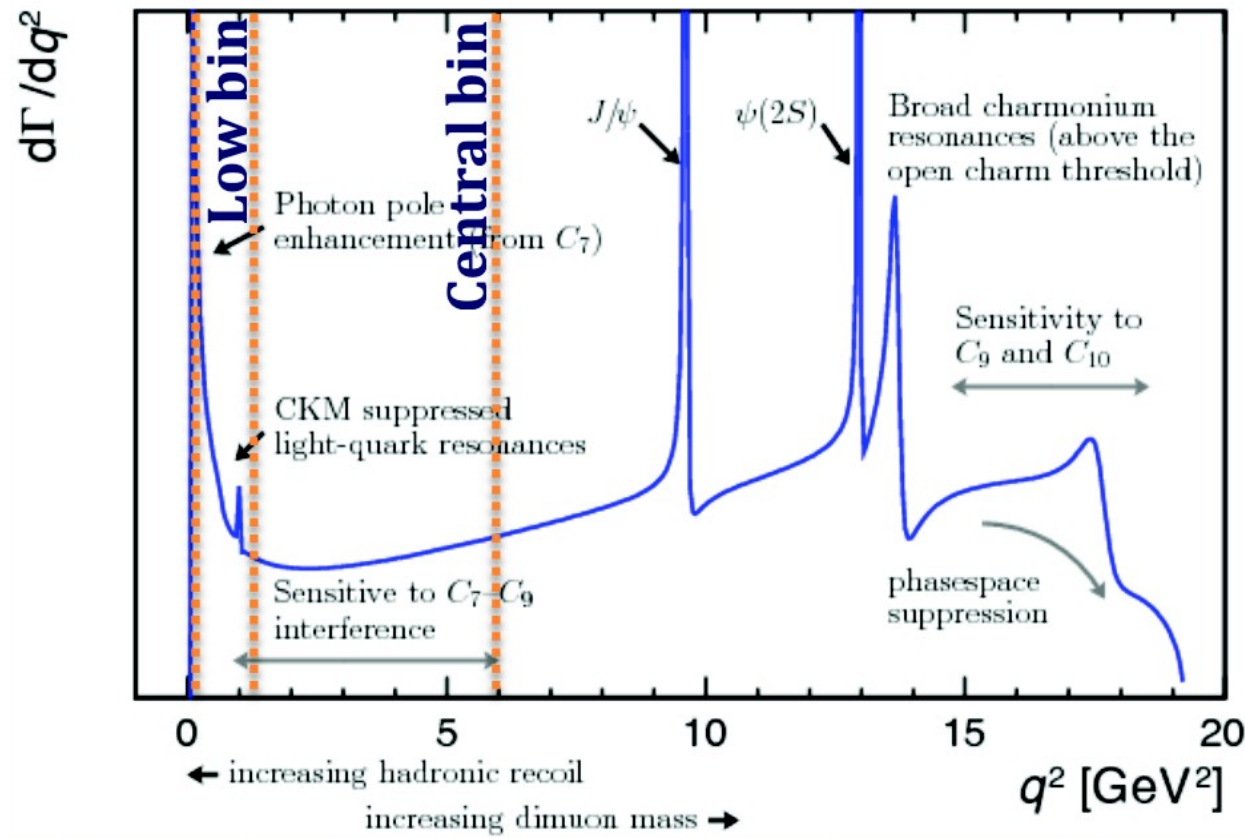
NP models which explain the observed discrepancies in the measurement of $R(K^{*})$ w.r.t SM predictions, foresee anomalous behaviors also in the angular distribution of the decay $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

Decay amplitude can be described using q^2 and three angles: θ_l , θ_K , ϕ :



Decay amplitude of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

$$\frac{1}{d(\Gamma+\bar{\Gamma})/dq^2} \frac{d^4(\Gamma+\bar{\Gamma})}{d\Omega d^3q^2} = \frac{9}{32\pi} \left[\frac{3}{4} (1 - F_L) \sin^2 \theta_k + F_L \cos^2 \theta_k \right. \\
+ \frac{1}{4} (1 - F_L) \sin^2 \theta_k \cos 2\theta_\ell - F_L \cos^2 \theta_k \cos 2\theta_\ell \\
+ S_3 \sin^2 \theta_k \sin^2 \theta_\ell \cos 2\phi + S_4 \sin 2\theta_k \sin 2\theta_\ell \cos \phi \\
+ S_5 \sin 2\theta_k \sin \theta_\ell \cos \phi + \frac{4}{3} A_{FB} \sin^2 \theta_k \cos \theta_\ell \\
+ S_7 \sin 2\theta_k \sin \theta_\ell \sin \phi + S_8 \sin 2\theta_k \sin 2\theta_\ell \sin \phi \\
\left. + S_9 \sin^2 \theta_k \sin^2 \theta_\ell \sin 2\phi \right],$$



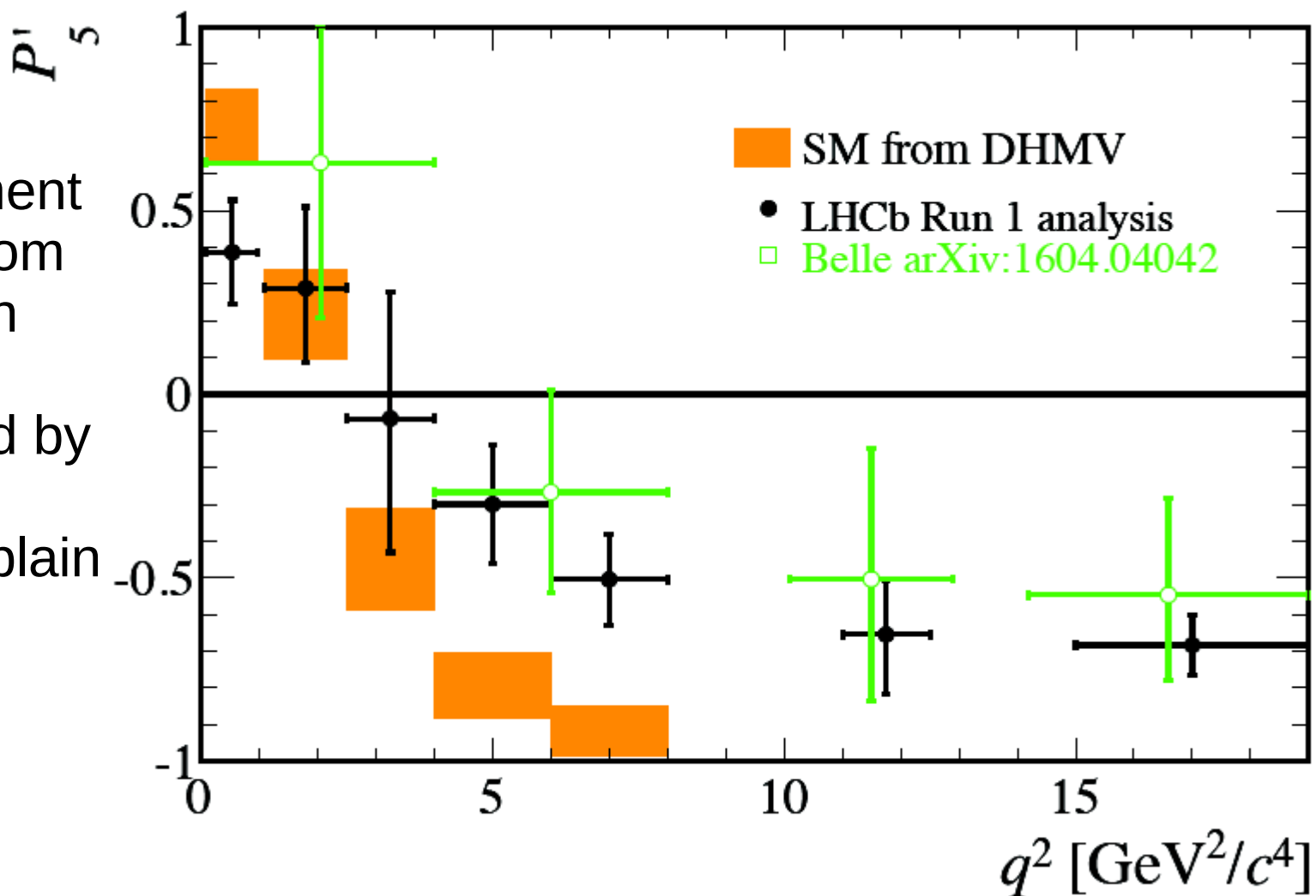
The P_5' anomaly

- Angular observable:

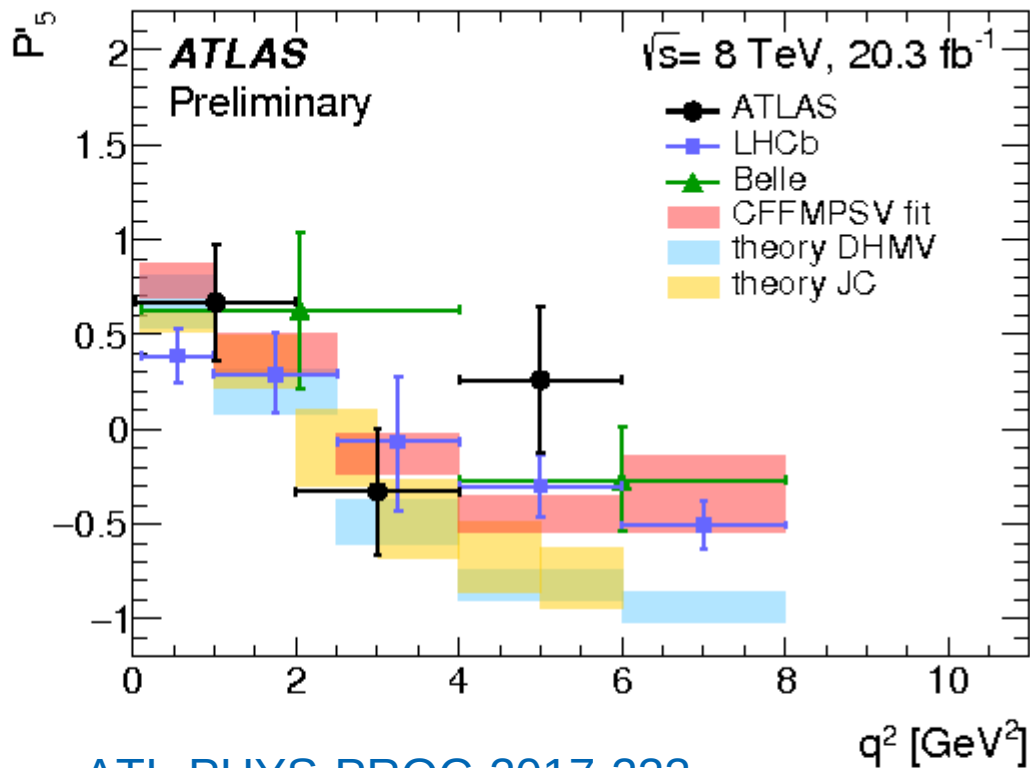
$$P_5' \equiv S_5 / \sqrt{F_L(1 - F_L)}$$

JHEP 02 (2016) 104

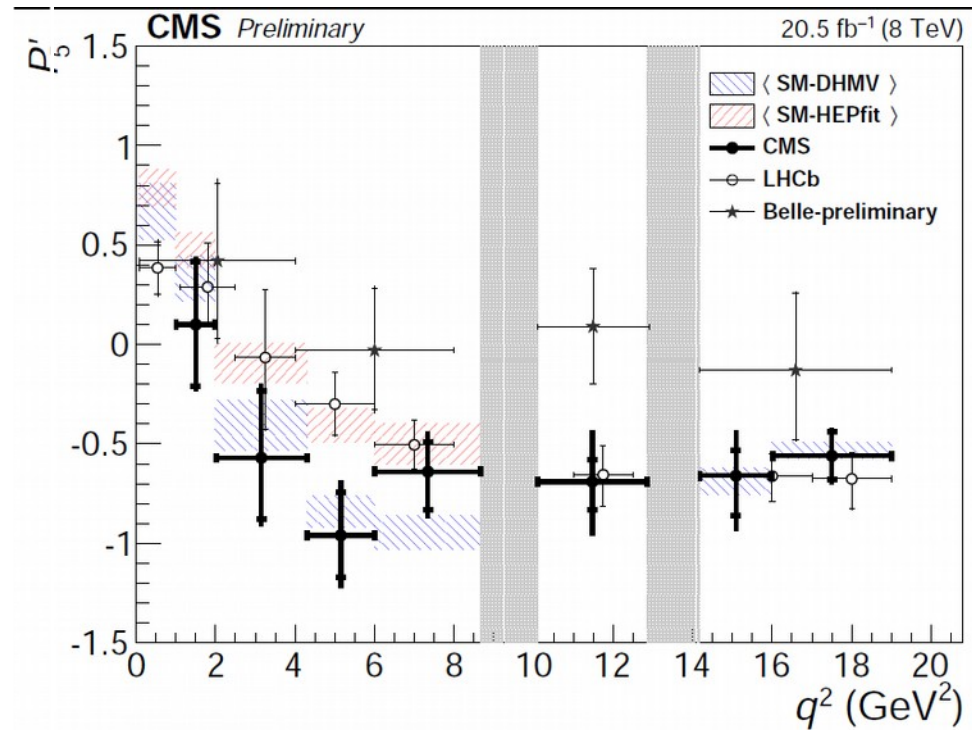
- LHCb measurement differs by 3.4σ from the SM prediction
- Can be explained by
 - SM charm-loop effects (cannot explain tension in R_{K^*})
 - New Physics



ATLAS and CMS results on P_5'



ATL-PHYS-PROC-2017-233
 arXiv:1710.11000 [hep-ex]



CMS-PAS-BPH-15-008

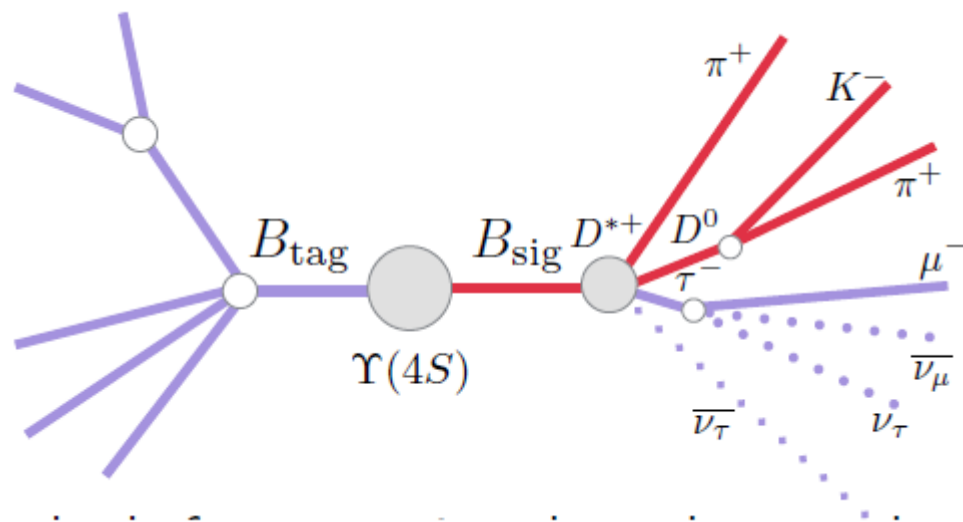
ATLAS measurement differs by 2.7σ from the SM prediction
 CMS results are consistent with SM prediction and other measurements

Measurement of R_{D^*}

B factories

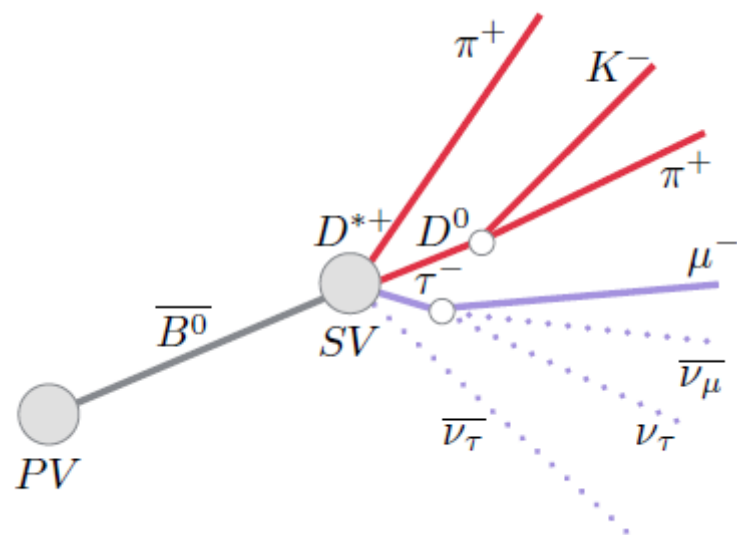
$$e^+e^- \rightarrow Y(4S) \rightarrow B^+B^-(B^0\bar{B}^0)$$

- Reconstruction of other B
- Clean signal but low efficiency



LHCb

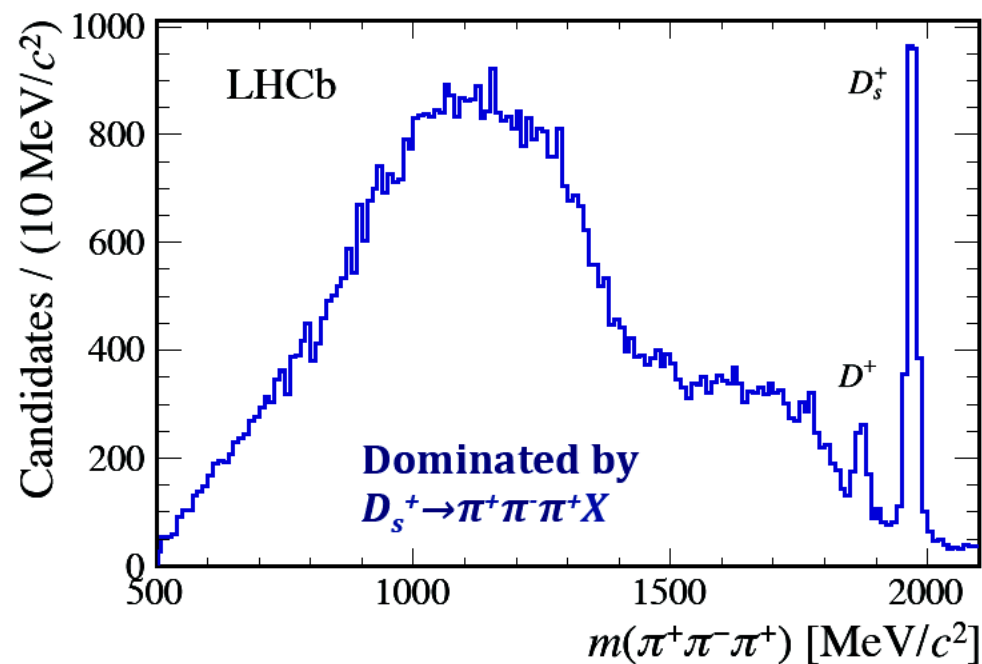
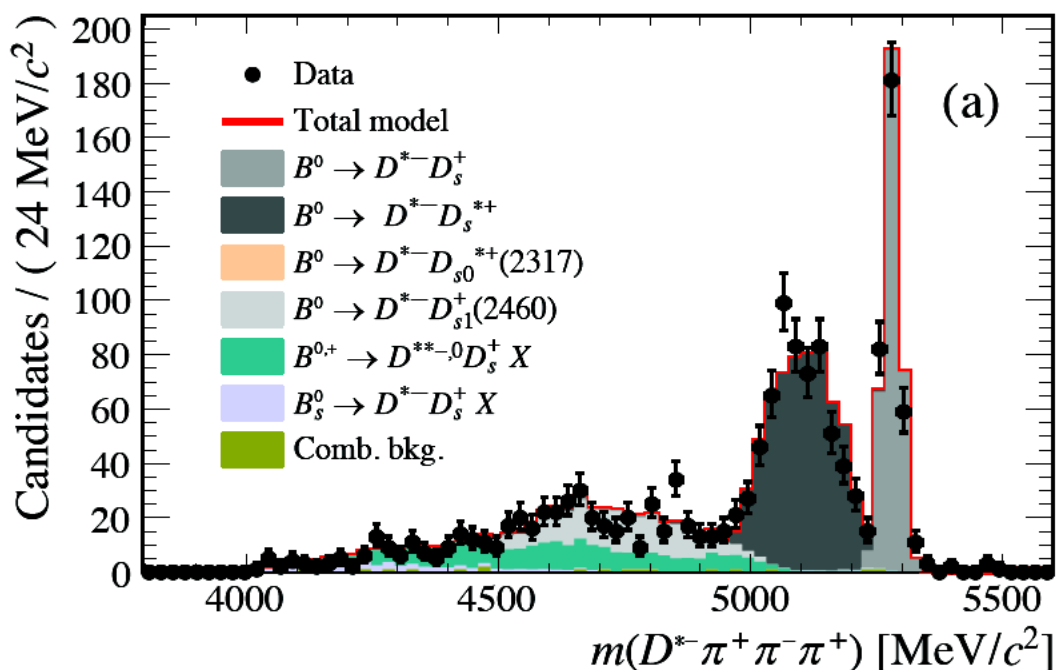
- Large boost, flight direction determined by PV & SV
- Huge B production



R_{D^*} in hadronic τ decays

Main systematic uncertainties due to:

- Size of simulated sample
- Shape of the background $B \rightarrow D^{*-} D_s^+ X$
- $D_{(s)}^+ \rightarrow \pi^+ \pi^- \pi^+ X$ decay mode. BESII future measurement will reduce it. Improvement as well of the upgraded ECAL
- Branching fraction of normalisation mode $B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+$ known with $\sim 4\%$ precision. Belle II can measure it precisely



R_{D^*} in muonic channels

