

# Fermion-mixing parameters and search limit on the mass leptoquark.

A.V. Povarov

YSU and YHMC AAC

The XXIII International Workshop  
High Energy Physics and Quantum Field Theory  
Yaroslavl, Russia, June 26 - July 3, 2017

# Outline

- 1 Introduction
- 2 Minimal Quark-Lepton Symmetry Model
- 3 Decays  $K^0$ -meson
- 4 Decays  $B^0$ - and  $B_s$ -meson
- 5 Conclusions

# Introduction

Vector Leptoquarks  $V_\alpha$  predicted in “four color” symmetry—  
J.C.Pati and A.Salam, PRD 10 1974

The restriction on the mass of the vector leptoquark from decays type

$$K_L^0 \rightarrow \mu^\pm e^\mp$$

are strong [order  $10^3$  TeV ](excluding fermion mixing).

- G. Valencia and S. Willenbrock, PRD 50, 1994
- A .V. Kuznetsov and N.V. Mikheev, PLB 329, 1994; YaF 58, 1995

The fermion mixing can be this restriction weak

- A. Povarov and A. Smirnov, ITEPh-talk, 2011
- A .V. Kuznetsov, N.V. Mikheev, A.V.Serghienko  
Int.J.Mod.Phys A27, 2012

# Minimal Quark-Lepton Symmetry Model

$$SU_V(4) \times SU_L(2) \times U_R(1)$$

A. D. Smirnov, Phys. Lett. B 346, (1995); YaF 58, (1995).

$$Q'^{L,R}_{ia\alpha} = \sum_j (A_{Q_a}^{L,R})_{ij} Q^{L,R}_{ja\alpha}, \quad I'^{L,R}_{ia} = \sum_j (A_{I_a}^{L,R})_{ij} I^{L,R}_{ja}$$

where  $i, j = 1, 2, 3$  – fermion generation indexes,  $a = 1, 2$  and  $\alpha = 1, 2, 3$  – indexes  $SU_L(2)$  and  $SU_c(3)$ .

$$A_{Q_a}^{L,R}, \quad A_{I_a}^{L,R}$$

- unitary matrices describe the fermion mixing and diagonalize the mass matrices of quarks and leptons, which appear after spontaneous symmetry breaking

$$C_Q = (A_{Q_1}^L)^+ A_{Q_2}^L = V_{CKM}, \quad C_I = (A_{I_1}^L)^+ A_{I_2}^L = U_{PMNS}^+$$

$$K_a^{L,R} = (A_{Q_a}^{L,R})^+ A_{I_a}^{L,R}$$

# Minimal Quark-Lepton Symmetry Model

The lagrangian interaction vector leptoquarks with down fermions can be written in the following form

$$L_{VdI} = \frac{g_4}{\sqrt{2}} (\bar{d}_{p\alpha} [(\mathcal{K}_2^L)_{pi} \gamma^\mu P_L + (\mathcal{K}_2^R)_{pi} \gamma^\mu P_R] l_i) V_{\alpha\mu} + h.c.,$$

where  $g_4 = g_{st}(M_c)$  is the  $SU_V(4)$  gauge coupling constant, related to the strong coupling constant at the mass scale  $M_c$  of the  $SU_V(4)$  symmetry breaking,  $p, i = 1, 2, 3, \dots$  are the quark and lepton generation indexes,  $\alpha = 1, 2, 3 - SU(3)$  colour index,  $P_{L,R} = (1 \pm \gamma_5)/2$ .

# Decays $K^0$ -meson

A. D. Smirnov, Mod.Phys. Lett. A 22, (2007); YaF 71, (2008).

$$BR(K_L^0 \rightarrow l_i^+ l_j^-) = \frac{m_{K^0} \pi \alpha_{st}^2 f_{K^0}^2 \bar{m}_{K^0}^2 (R_{K^0}^V)^2}{4 m_V^4 \Gamma_K^{total}} |k_{ij}^{(K^0)}|^2,$$

where  $\bar{m}_{K^0} = m_{K^0}^2 / (m_s + m_d)$ ,  $\Gamma_K^{total}$  – total width decay  $K_L^0$ -meson,  $f_{K^0} = 0.16$  GeV – form factor  $K_L^0$ -meson, factor  $R_{K^0}^V = R_{K^0}(\mu_{K^0}, M_C)$  incorporate gluonic corrections, mixing factors incorporate fermionic mixing in general form

$$\begin{aligned} k_{ij}^{(K^0)} &= \sqrt{(|\varkappa_{ij}^L|^2 + |\varkappa_{ij}^R|^2)/2} \\ \varkappa_{ij}^{L,R} &= (K_2^{L,R})_2 (\overset{*}{K}_2^{R,L})_{1j} + (K_2^{L,R})_1 (\overset{*}{K}_2^{R,L})_{2j}. \end{aligned}$$

# Decays $K^0$ -meson

PDG: C. Patrignani et al., Chin. Phys. C, 40, 100001 (2016) and 2017.

$$BR(K_L^0 \rightarrow e^\pm \mu^\mp) < 4.7 \times 10^{-12}$$

$$BR(K_L^0 \rightarrow \mu^+ \mu^-) = (6.8 \pm 0.11) \times 10^{-9}$$

$$BR(K_L^0 \rightarrow e^+ e^-) = (9_{-4}^{+6}) \times 10^{-12}.$$

$$K_2^{L,R} =$$

$$\begin{bmatrix} c_{12}^{L,R} c_{13}^{L,R} & s_{12}^{L,R} c_{13}^{L,R} & s_{13}^{L,R} e^{-i\delta_{L,R}} \\ s_{12}^{L,R} c_{23}^{L,R} - c_{12}^{L,R} s_{23}^{L,R} s_{13}^{L,R} e^{i\delta_{L,R}} & c_{12}^{L,R} c_{23}^{L,R} - s_{12}^{L,R} s_{23}^{L,R} s_{13}^{L,R} e^{i\delta_{L,R}} & s_{23}^{L,R} c_{13}^{L,R} \\ s_{12}^{L,R} s_{23}^{L,R} - c_{12}^{L,R} c_{23}^{L,R} s_{13}^{L,R} e^{i\delta_{L,R}} & c_{12}^{L,R} s_{23}^{L,R} - s_{12}^{L,R} c_{23}^{L,R} s_{13}^{L,R} e^{i\delta_{L,R}} & c_{23}^{L,R} c_{13}^{L,R} \end{bmatrix}.$$

$$s_{ij}^{L,R} = \sin \Theta_{ij}^{L,R}, c_{ij}^{L,R} = \cos \Theta_{ij}^{L,R}$$

$$M_{Vij} = f(BR(K^0 \rightarrow l_i l_j), \Theta_{ij}^{L,R}, \delta_{L,R})$$

# Decays $K^0$ -meson

Joint calculation of mass vector leptoquark from the three decay  $K_L^0$  - meson taking into account additional fermion mixing give the lower bounds to 0.

In particular, the choice of parameters in next values:

$\Theta_{12}^L = \Theta_{13}^L = \Theta_{23}^L = \Theta_{12}^R = \Theta_{13}^R = \Theta_{23}^R = \pi/2$ , with correspondent matrix

$$K_2^L = K_2^R = \begin{bmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{bmatrix},$$

obtain  $k_{21}^{(K^0)} = k_{11}^{(K^0)} = k_{22}^{(K^0)} = 0$ , and experimental limits performed for all values  $m_V$ .

# Decays $K^0$ - and $B^0$ -mesons

$$BR(B^0 \rightarrow l_i^+ l_j^-) = \frac{m_{B^0} \pi \alpha_{st}^2 f_{B^0}^2 \bar{m}_{B^0}^2 (R_{B^0}^V)^2}{4 m_V^4 \Gamma_B^{total}} |k_{ij}^{(B^0)}|^2,$$

where  $\bar{m}_{B^0} = m_{B^0}^2 / (m_b + m_d)$ ,  $f_{B^0} = 0.229$  GeV – form factor  $B^0$ -meson, factor  $R_{B^0}^V = R_{B^0}(\mu_{B^0}, M_C)$  incorporate gluonic corrections,  $\mu_{l_i^\pm} = m_{l_i^\pm} / (m_{B^0} R_{B^0}^V)$

$$\begin{aligned} |k_{ij}^{(B^0)}|^2 &= \left[ (|\beta_{ij}^L|^2 + |\beta_{ij}^R|^2)(1 - \mu_{l_i}^2 - \mu_{l_j}^2) + 2(\beta_{ij}^* \beta_{ij}^R + \beta_{ij}^L \beta_{ij}^{*R}) \mu_{l_i} \mu_{l_j} \right] \\ &\times \sqrt{[1 - (\mu_{l_i} + \mu_{l_j})^2][1 - (\mu_{l_i} - \mu_{l_j})^2]}, \end{aligned} \quad (1)$$

$$\beta_{ij}^{L,R} = k_{ij}^{L,R} - (\mu_{l_j^-} k_{ij}'^{L,R} + \mu_{l_i^+} k_{ij}'^{R,L})/2$$

$$k_{ij}^{L,R} = (K_2^{L,R})_3 (\overset{*}{K}_2^{R,L})_{1j}, \quad k_{ij}'^{L,R} = (K_2^{L,R})_3 (\overset{*}{K}_2^{L,R})_{1j}$$

# Decays $K^0$ - and $B^0$ -mesons

$$\begin{aligned}
 BR(B^0 \rightarrow e^\pm \mu^\mp) &< 2.8 \times 10^{-9} \\
 BR(B^0 \rightarrow e^\pm \tau^\mp) &< 2.8 \times 10^{-5} (*) \\
 BR(B^0 \rightarrow \mu^\pm \tau^\mp) &< 2.2 \times 10^{-5} (*) \\
 BR(B^0 \rightarrow \mu^+ \mu^-) &< 3.4 \times 10^{-10} \\
 BR(B^0 \rightarrow e^+ e^-) &< 8.3 \times 10^{-8} \\
 BR(B^0 \rightarrow \tau^+ \tau^-) &< 2.1 \times 10^{-3}.
 \end{aligned}$$

LHCb collaboration: R. Aaij et al, Phys.Rev.Lett. 118 (2017)

The restriction on the mass VLQ obtained from decays  $K_L^0$  and  $B^0$  mesons **together** are 10 TeV

# Decays $K^0_-$ , $B^0_-$ and $B_s$ -mesons

$$BR(B_s \rightarrow e^\pm \mu^\mp) < 1.1 \times 10^{-8} (*)$$

$$BR(B_s \rightarrow \mu^+ \mu^-) = (3.0^{+0.67}_{-0.63}) \times 10^{-10} (*)$$

$$BR(B_s \rightarrow e^+ e^-) < 8.3 \times 10^{-8}$$

$$BR(B_s \rightarrow \tau^+ \tau^-) < 6.8 \times 10^{-3}$$

LHCb collaboration: R. Aaij et al, Phys.Rev.Lett. 118 (2017)

For example if set parameters as

$$\Theta_{12}^L = \Theta_{12}^R = 9\pi/50, \quad \Theta_{13}^L = \Theta_{13}^R = \pi/2, \quad \Theta_{23}^L = \Theta_{23}^R = 0,$$

$$K_2^L = K_2^R = \begin{pmatrix} 0 & 0 & 1 \\ -0.54 & 0.84 & 0 \\ -0.84 & -0.54 & 0 \end{pmatrix}. \quad (2)$$

# Decays $K^0_L$ , $B^0$ and $B_s$ -mesons

$$\begin{aligned} k_{ij}^{(K^0)} &= \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}, \\ k_{ij}^{(B^0)} &= \begin{pmatrix} 0 & 0 & 0.87 \\ 0 & 0 & 0.35 \\ 0 & 0 & 0 \end{pmatrix}, \\ k_{ij}^{(B_s)} &= \begin{pmatrix} 0.41 & 0.99 & 0 \\ 0.16 & 0.4 & 0 \\ 0 & 0 & 0 \end{pmatrix}. \end{aligned}$$

The restriction on the mass vector leptoquark obtained from decays  $K^0_L$ ,  $B^0$  and  $B_s$  mesons together are 85 TeV

# Conclusions

- Accounting fermion mixing in leptonic decays of  $K_L^0$ ,  $B^0$  and  $B_s$  mesons leads to a significant weakening of restrictions on mass vector leptoquark. The current limit is about 85 TeV, it is essentially weaker, than restriction without taking into account fermion mixing.

# Conclusions

- Accounting fermion mixing in leptonic decays of  $K_L^0$ ,  $B^0$  and  $B_s$  mesons leads to a significant weakening of restrictions on mass vector leptoquark. The current limit is about 85 TeV, it is essentially weaker, than restriction without taking into account fermion mixing.

$$M_V : 2200 \text{TeV} \rightarrow 85 \text{TeV}$$

We hope that the “Grand Desert” will not.