

# Domain Walls and Matter-Antimatter Domains in the Early Universe

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based on papers

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- The model
- Bounds on parameters
- Evolution of fields during inflation
- Generation of BAU
- Domain walls in expanding Universe

Lagrangian:

$$L = L_{\Phi} + L_{\chi} + L_{int},$$

where

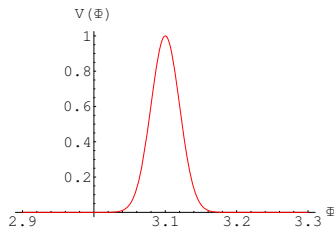
$$L_{\Phi} = \frac{1}{2}(\partial\Phi)^2 - \frac{1}{2}M^2\Phi^2,$$

$$L_{\chi} = \frac{1}{2}(\partial\chi)^2 - \frac{1}{2}m^2\chi^2 - \frac{1}{4}\lambda_{\chi}\chi^4,$$

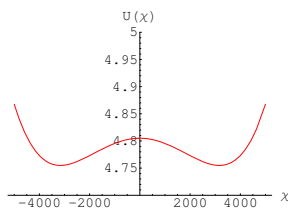
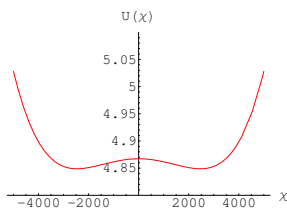
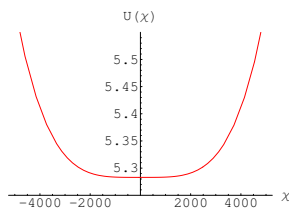
$$L_{int} = \mu^2\chi^2V(\Phi).$$

Potential shape:

$$V(\Phi) = \exp\left[-\frac{(\Phi - \Phi_0)^2}{2\Phi_1^2}\right],$$



$$U(\Phi, \chi) = \left( \frac{1}{2} m^2 - \mu^2 V(\Phi) \right) \chi^2 + \frac{1}{4} \lambda_\chi \chi^4 + \frac{1}{2} M^2 \Phi^2$$



$$\Phi = \Phi_0 + 2\Phi_1 \sqrt{\ln(\sqrt{2}\mu/m)}$$

$$m^2/2 - \mu^2 V(\Phi) = 0$$

$$\Phi = \Phi_0 + \Phi_1$$

$$\Phi = \Phi_0$$

$\Phi_0 = 3.1 m_{Pl}$ ,  $\Phi_1 = 0.02 m_{Pl}$ ,  $\mu = 10^{-4} m_{Pl}$ , and  $m = 10^{-10} m_{Pl}$ .

Field  $\chi$  is measured in units of  $M$ ,  $U(\Phi, \chi)$  is in units  $10^{-12} m_{Pl}^4$ .

Equations of motion:

$$\ddot{\Phi} + 3H\dot{\Phi} + M^2\Phi + \mu^2\chi^2 \frac{\Phi - \Phi_0}{\Phi_1^2} V(\Phi) = 0,$$

$$\ddot{\chi} + 3H\dot{\chi} + m^2\chi + \lambda_\chi\chi^3 - 2\mu^2\chi V(\Phi) = 0,$$

where  $H = \dot{a}/a$  is the Hubble parameter,  $a(t)$  is a scale factor, which enters the FLRW metric

$$ds^2 = dt^2 - a^2(t) d\mathbf{x}^2.$$

The Hubble parameter is defined by energy density  $\rho$

$$H = \sqrt{\frac{8\pi\rho}{3m_{Pl}^2}} = \sqrt{\frac{8\pi}{3m_{Pl}^2} \left( \frac{\dot{\Phi}^2}{2} + \frac{M^2\Phi^2}{2} + \frac{\dot{\chi}^2}{2} + \frac{m^2\chi^2}{2} + \frac{\lambda_\chi\chi^4}{4} - \mu^2\chi^2 V(\Phi) \right)},$$

where  $m_{Pl} \approx 1.2 \cdot 10^{19}$  GeV is the Planck mass.

- We do not want to break common inflation scenario:  
 $\Phi_{in} > 3.3m_{Pl}$ ,  $10^{-7}m_{Pl} < M < 10^{-6}m_{Pl}$ .
- The size of a domain should be large enough (at least 10 Mpc):  
 $\Phi_0 \approx 3.1m_{Pl}$
- $\chi$  should not noticeably affect the inflaton field:

$$M^2\Phi_0^2 \gg \mu^2 \chi^2|_{\Phi=\Phi_0} \sim \frac{\mu^4}{\lambda_\chi},$$

$$\mu^4 \ll M^2\Phi_0^2\lambda_\chi.$$

For  $M = 10^{-6}m_{Pl}$ ,  $\Phi_0 = 3.1m_{Pl}$  we obtain  $\mu \ll 1.8 \cdot 10^{-3}m_{Pl} \sqrt[4]{\lambda_\chi}$ .

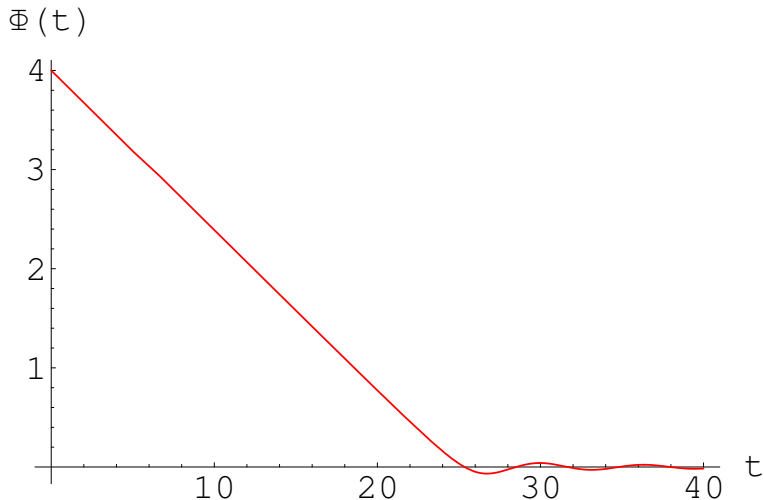
- $\chi$  should be able to reach the minimum:  
 $\chi \propto \exp(\mu t)$  for  $\mu \gg H = \sqrt{4\pi/3} M/m_{Pl} \Phi \sim 6 \cdot 10^{-6}m_{Pl}$

$$\mu\tau = \mu \frac{8\sqrt{3\pi}\Phi_1}{Mm_{Pl}} \gtrsim \ln \frac{\eta_{max}}{\chi_{in}} = \frac{1}{2} \ln \frac{2\mu^2}{\lambda_\chi\chi_{in}^2},$$

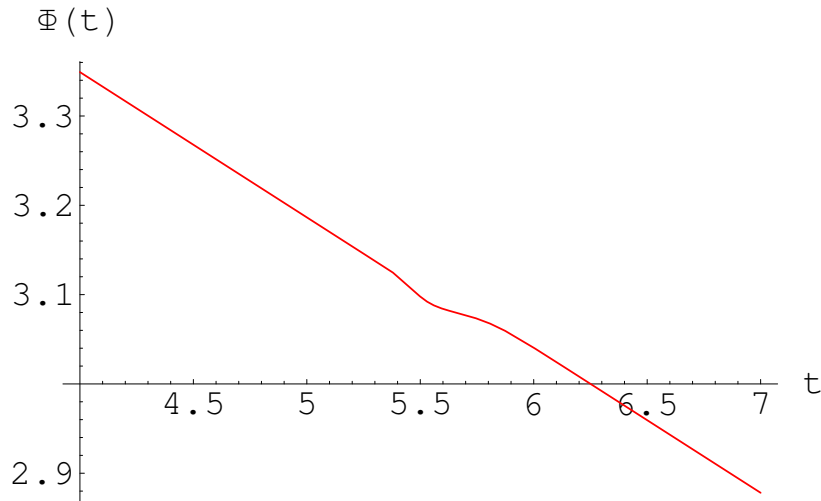
$$\mu \gtrsim \frac{Mm_{Pl}}{16\sqrt{3\pi}\Phi_1} \ln \frac{2\mu^2}{\lambda_\chi\chi_{in}^2}.$$

- Field  $\chi$  should slowly decrease with time after vanishing of  $V(\Phi)$ :  
 If  $\lambda_\chi\chi^3$  dominates in equations of motion then  $\chi = \sqrt{\frac{3H}{2\lambda_\chi}} \frac{1}{\sqrt{t-C}}$

$$\Phi_{in} = 4, \Phi_0 = 3.1, \Phi_1 = 0.02, M = 10^{-6}, \chi_{in} = 10^{-6}, m = 10^{-10}, \lambda_\chi = 2 \cdot 10^{-3}, \mu = 10^{-4}.$$



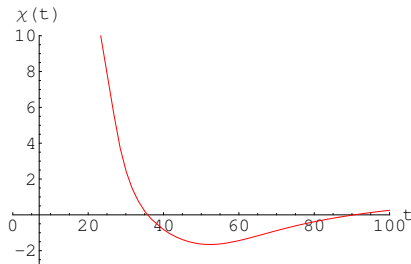
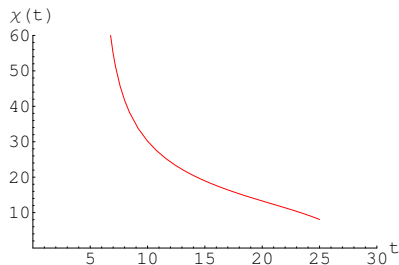
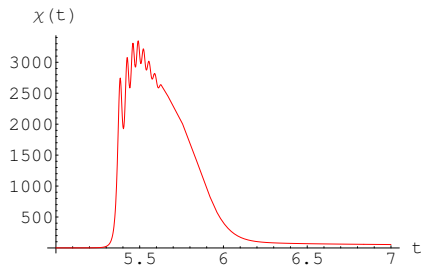
$$\Phi_{in} = 4, \Phi_0 = 3.1, \Phi_1 = 0.02, M = 10^{-6}, \chi_{in} = 10^{-6}, m = 10^{-10}, \lambda_\chi = 2 \cdot 10^{-3}, \mu = 10^{-4}.$$





# Evolution of $\chi$

$\Phi_{in} = 4, \Phi_0 = 3.1, \Phi_1 = 0.02, M = 10^{-6}, \chi_{in} = 10^{-6}, m = 10^{-10}, \lambda_\chi = 2 \cdot 10^{-3}, \mu = 10^{-4}$ .



$$L_{free} = \bar{\psi}^k i \hat{\partial} \psi^k - m_{\psi kl} \bar{\psi}^k \psi^l = \bar{\psi}_R^k i \hat{\partial} \psi_R^k + \bar{\psi}_L^k i \hat{\partial} \psi_L^k - m_{\psi kl} (\bar{\psi}_R^k \psi_L^l + \bar{\psi}_L^k \psi_R^l).$$

$$L_{\chi\psi\psi} = g_{kl} \chi \bar{\psi}^k i \gamma_5 \psi^l = g_{kl} \chi (\bar{\psi}_R^k i \gamma_5 \psi_L^l + \bar{\psi}_L^k i \gamma_5 \psi_R^l) = i g_{kl} \chi (\bar{\psi}_L^k \psi_R^l - \bar{\psi}_R^k \psi_L^l).$$

$$L_{free} + L_{\chi\psi\psi} = \bar{\psi}_R i \hat{\partial} \psi_R + \bar{\psi}_L i \hat{\partial} \psi_L - (\bar{\psi}_R M_\psi \psi_L + \bar{\psi}_L M_\psi^\dagger \psi_R),$$

where  $M_\psi = m_\psi + i g \chi$ .

With two unitary transformations,  $\psi_R \rightarrow \psi'_R = U_R \psi_R$  and  $\psi_L \rightarrow \psi'_L = U_L \psi_L$ , it is always possible to diagonalize mass matrix:

$$L'_{free} = \bar{\psi}^a i \hat{\partial} \psi^a - m'_{\psi ab} \bar{\psi}^a \psi^b,$$

If there is an interaction with a vector boson  $X$ :

$$g_{Rkl} X_\mu \bar{\psi}_R^k \gamma^\mu \psi_R^l + g_{Lkl} X_\mu \bar{\psi}_L^k \gamma^\mu \psi_L^l \rightarrow g'_{Rab} X_\mu \bar{\psi}_R^a \gamma^\mu \psi_R^b + g'_{Lab} X_\mu \bar{\psi}_L^a \gamma^\mu \psi_L^b.$$

Asymmetry:

$$\Delta_B \sim \delta \frac{h}{g_X} \left( \frac{m_{th}}{m_{Pl}} \right)^{1/2} \Rightarrow \text{for } h/g_X \sim 1, m_{th} \sim M \text{ we get } \delta \sim 10^{-7}$$

$$ds^2 = dt^2 - e^{2Ht} (dx^2 + dy^2 + dz^2).$$

$$\mathcal{L} = \frac{1}{2} g^{\mu\nu} \partial_\mu \varphi \partial_\nu \varphi - \frac{\lambda}{2} (\varphi^2 - \eta^2)^2.$$

$H = 0$ , one-dimensional case ( $\varphi = \varphi(z)$ ):

$$\frac{d^2 \varphi}{dz^2} = 2\lambda \varphi (\varphi^2 - \eta^2).$$

Solution (wall at  $z = 0$ ):

$$\varphi(z) = \eta \tanh \frac{z}{\delta_0},$$

where  $\delta_0 = 1/(\sqrt{\lambda}\eta)$  is the width.

$H > 0$ , stationary solutions ( $\varphi$  depends only on  $za(t)$ ):

Basu, Vilenkin, Phys. Rev. D 50 (1994) 7150

$$\varphi = \eta \cdot f(u), \quad \text{where } u = Hze^{Ht}.$$

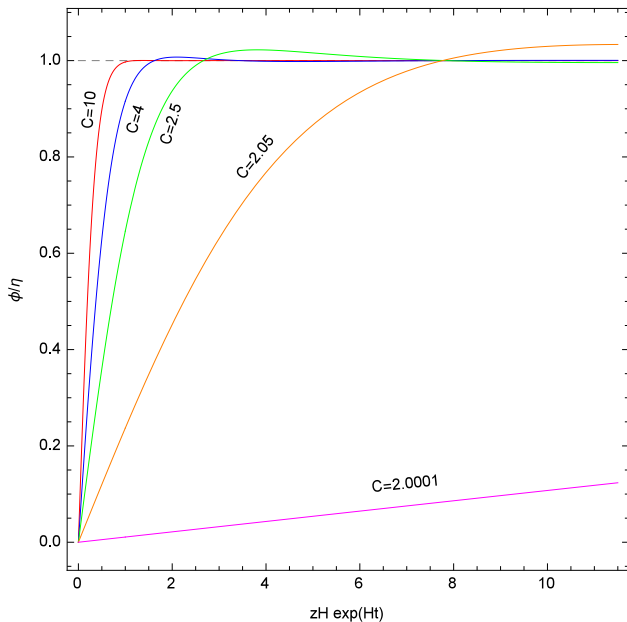
Equation of motion:

$$(1 - u^2) f'' - 4uf' = -2Cf(1 - f^2),$$

where  $C = 1/(H\delta_0)^2 = \lambda\eta^2/H^2 > 0$ .

Boundary conditions:  $f(0) = 0, f(\pm\infty) = \pm 1$ .

# Stationary solutions



$$\frac{\partial^2 \varphi}{\partial t^2} + 3H \frac{\partial \varphi}{\partial t} - e^{-2Ht} \frac{\partial^2 \varphi}{\partial z^2} = -2\lambda \varphi (\varphi^2 - \eta^2).$$

With the dimensionless variables  $\tau = Ht$ ,  $\zeta = Hz$ ,  $f(\zeta, \tau) = \varphi(z, t)/\eta$ :

$$\frac{\partial^2 f}{\partial \tau^2} + 3 \frac{\partial f}{\partial \tau} - e^{-2\tau} \frac{\partial^2 f}{\partial \zeta^2} = 2Cf(1 - f^2),$$

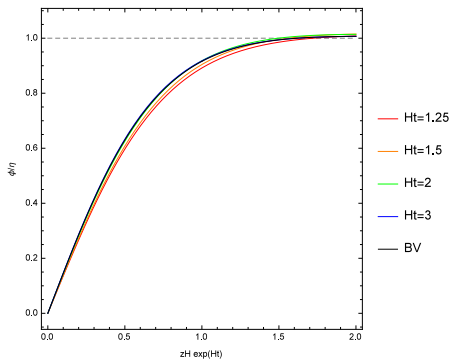
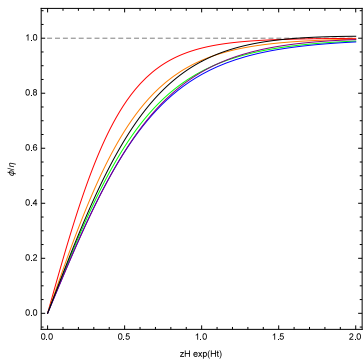
where  $C = \lambda\eta^2/H^2 = 1/(H\delta_0)^2 > 0$ .

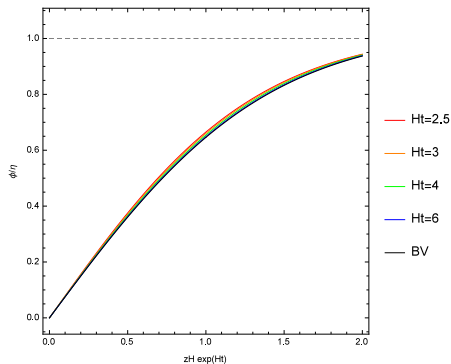
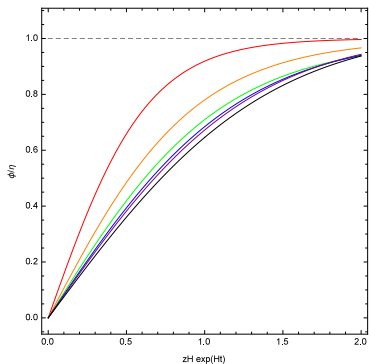
Boundary conditions:

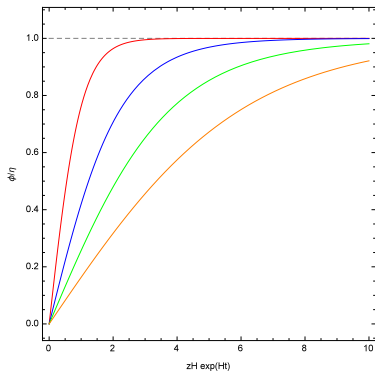
$$f(0, \tau) = 0, \quad f(\pm\infty, \tau) = \pm 1,$$

Starting conditions:

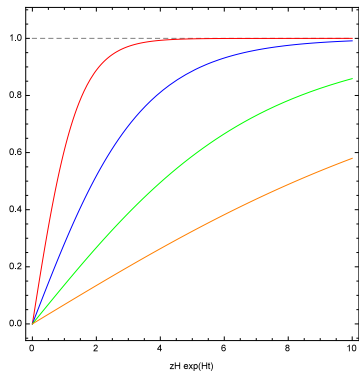
$$f(\zeta, 0) = \tanh \frac{z}{\delta_0} = \tanh \sqrt{C}\zeta, \quad \left. \frac{\partial f(\zeta, \tau)}{\partial \tau} \right|_{\tau=0} = 0.$$





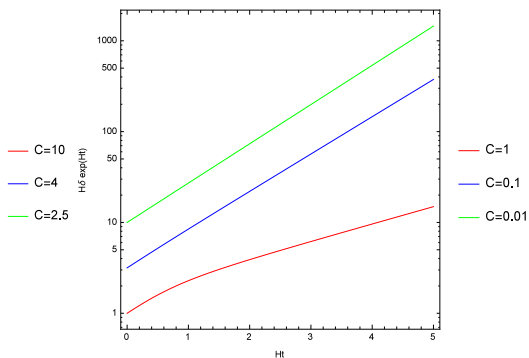
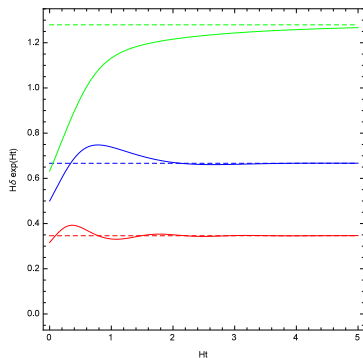
 $C = 1$ 

—  $Ht=0$   
—  $Ht=1$   
—  $Ht=2$   
—  $Ht=3$

 $C = 0.5$ 

—  $Ht=0$   
—  $Ht=1$   
—  $Ht=2$   
—  $Ht=3$





- The scenario for generation of matter-antimatter domains (separated by cosmologically large distances) is suggested:
  - We found bounds on parameters at which this scenario can be realized.
  - The numerical simulation was performed to demonstrate that this scenario is possible.
  
- The evolution of a domain wall in the de Sitter space was studied:
  - In case  $C = \lambda\eta^2/H^2 = 1/(H\delta_0)^2 > 2$  the solution tends to the stationary one.
  - In case  $C = \lambda\eta^2/H^2 = 1/(H\delta_0)^2 < 2$  the solution is quickly expands. For  $C \lesssim 0.1$  the growth of the width becomes almost exponential, i.e. the wall expands with the Universe.