

# Double Higgs boson production with isotriplet scalars

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based on

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(see talk by M. Flechl)

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Large integrated luminosity is required so  $2h$  production will not be found in the nearest future at LHC, **if there is no New Physics.**

$$\Phi \equiv \begin{bmatrix} \Phi^+ \\ \Phi^0 \end{bmatrix} \equiv \begin{bmatrix} \Phi^+ \\ \frac{1}{\sqrt{2}}(v + \varphi + i\chi) \end{bmatrix}, \quad \Delta \equiv \frac{\vec{\Delta}\vec{\sigma}}{\sqrt{2}} \equiv \begin{bmatrix} \frac{\delta^+}{\sqrt{2}} & \delta^{++} \\ \delta^0 & -\frac{\delta^+}{\sqrt{2}} \end{bmatrix}, \quad \delta^0 = \frac{v_\Delta + \delta + i\eta}{\sqrt{2}}.$$

$$\begin{aligned} \mathcal{L} = & |D_\mu \Phi|^2 + \frac{1}{2} m_\Phi^2 (\Phi^\dagger \Phi) - \frac{\lambda}{2} (\Phi^\dagger \Phi)^2 + \\ & + \text{Tr} \left[ (D_\mu \Delta)^\dagger (D_\mu \Delta) \right] - M_\Delta^2 \text{Tr} \left[ \Delta^\dagger \Delta \right] - \\ & - \frac{\mu}{\sqrt{2}} \left( \Phi^T i\sigma^2 \Delta^\dagger \Phi + h.c. \right) - \\ & - \frac{1}{\sqrt{2}} \left( Y_{\Delta ij} \bar{L}_i i\sigma^2 \Delta C \bar{L}_j + h.c. \right), \end{aligned}$$

Neutrino mass matrix  $M_{ij} = v_\Delta Y_{\Delta ij}$ .

$Y_\Delta$  is large,  $v_\Delta$  is small  
 (neutrino masses are small due to smallness of  $v_\Delta$  - “natural” case)

Coupling of  $\Delta$  to  $Z, W, h$ :  $\propto v_\Delta$

Coupling of  $\Delta$  to fermions:  $\propto \frac{m_\nu}{v_\Delta}$

Mode  $\Delta^0 \rightarrow \nu\nu$  dominates in  $\Delta^0$  decays

Mode  $\Delta^{++} \rightarrow l^+l^+$  dominates in  $\Delta^{++}$  decays

Search for  $\Delta^{++}$ :

$$Z^0/\gamma \rightarrow \Delta^{++}\Delta^{--} \rightarrow l^+l^+l^-l^-$$

↓

$M_\Delta > 400$  GeV according to LHC data

$Y_\Delta$  is small,  $v_\Delta$  is large  
(neutrino masses are small due to smallness of  $Y_\Delta$  - lack of “naturalness”)

Diboson decays dominate in  $\Delta^0, \Delta^{++}$  decays

Search for  $\Delta^{++}$ :  $M_\Delta \gtrsim 100\text{GeV}$

$$\mathcal{L}_{V^2} = g^2 |\delta^0|^2 W^+ W^- + \frac{1}{2} g^2 |\Phi^0|^2 W^+ W^- + \bar{g}^2 |\delta^0|^2 Z^2 + \frac{1}{4} \bar{g}^2 |\Phi^0|^2 Z^2.$$

$$\begin{cases} M_W^2 &= \frac{g^2}{4} (v^2 + 2v_\Delta^2), \\ M_Z^2 &= \frac{\bar{g}^2}{4} (v^2 + 4v_\Delta^2). \end{cases}$$

$$v^2 + 2v_\Delta^2 = (246 \text{ GeV})^2,$$

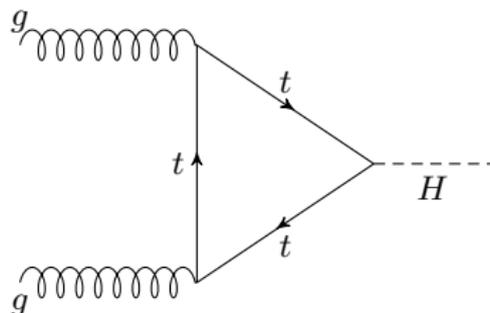
$$\frac{M_W}{M_Z} \approx \left( \frac{M_W}{M_Z} \right)_{\text{SM}} \left( 1 - \frac{v_\Delta^2}{v^2} \right).$$

$$v_\Delta < 5 \text{ GeV}$$

$$V(\varphi, \delta) = \frac{1}{2}\lambda v^2\varphi^2 + \frac{1}{2}M_\Delta^2\delta^2 - \mu v\varphi\delta = \frac{1}{2} \begin{bmatrix} \varphi & \delta \end{bmatrix} \begin{bmatrix} \lambda v^2 & -\mu v \\ -\mu v & M_\Delta^2 \end{bmatrix} \begin{bmatrix} \varphi \\ \delta \end{bmatrix}$$

$$\begin{bmatrix} h \\ H \end{bmatrix} = \begin{bmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{bmatrix} \begin{bmatrix} \varphi \\ \delta \end{bmatrix}$$

$$\tan 2\alpha = \frac{4v_\Delta}{v} \frac{M_\Delta^2}{M_\Delta^2 - \lambda v^2}$$



$$\underline{v_\Delta = 5 \text{ GeV}, \quad M_H = 300 \text{ GeV}}$$

$$\sin^2 \alpha \approx [(2v_\Delta/v) / (1 - M_h^2/M_H^2)]^2 \approx 2.4 \cdot 10^{-3}$$

## gluon fusion

$M_h$ (GeV)	125	300
$\sigma_{gg \rightarrow h}$ (pb)	$49.97 \pm 10\%$	$11.07 \pm 10\%$
$M_H$ (GeV)	X	300
$\sigma_{gg \rightarrow H}$ (fb)	X	$25 \pm 10\%$

## vector boson fusion

$$\sigma_{ZZ \rightarrow H} = \left( \frac{2v_\Delta}{v} \frac{1 - 2M_h^2/M_H^2}{1 - M_h^2/M_H^2} \right)^2 \times (\sigma_{ZZ \rightarrow h})^{\text{SM}} \approx 10^{-3} \times (\sigma_{ZZ \rightarrow h})^{\text{SM}}$$

$$\sigma_{ZZ \rightarrow H} = 0.365(1) \text{ fb}$$

$$\Gamma_{H \rightarrow hh} = \frac{v_\Delta^2}{v^4} \frac{M_H^3}{8\pi} \left[ \frac{1 + 2 \left( \frac{M_h}{M_H} \right)^2}{1 - \left( \frac{M_h}{M_H} \right)^2} \right]^2 \sqrt{1 - 4 \frac{M_h^2}{M_H^2}}, \quad 77\%$$

$$\Gamma_{H \rightarrow ZZ} = \frac{v_\Delta^2}{v^4} \frac{M_H^3}{8\pi} \left[ \frac{1 - 2 \left( \frac{M_h}{M_H} \right)^2}{1 - \left( \frac{M_h}{M_H} \right)^2} \right]^2 \left( 1 - 4 \frac{M_Z^2}{M_H^2} + 12 \frac{M_Z^4}{M_H^4} \right) \sqrt{1 - 4 \frac{M_Z^2}{M_H^2}}, \quad 19\%$$

$$\Gamma_{H \rightarrow WW} = \frac{v_\Delta^2}{v^4} \frac{M_H^3}{4\pi} \left[ \frac{M_h^2/M_H^2}{1 - \left( \frac{M_h}{M_H} \right)^2} \right]^2 \left( 1 - 4 \frac{M_W^2}{M_H^2} + 12 \frac{M_W^4}{M_H^4} \right) \sqrt{1 - 4 \frac{M_W^2}{M_H^2}}, \quad 3\%$$

$$\Gamma_{H \rightarrow gg} = \frac{v_\Delta^2}{v^4} \frac{M_H^3}{2\pi} \left( \frac{\alpha_s}{3\pi} \right)^2 \left( 1 - \frac{M_h^2}{M_H^2} \right)^{-2}, \quad 0.05\%$$

$$\Gamma_{H \rightarrow t\bar{t}} = \frac{v_\Delta^2}{v^4} \frac{N_c m_t^2 M_H}{2\pi} \frac{1}{(1 - M_h^2/M_H^2)^2} \left( 1 - 4 \frac{m_t^2}{M_H^2} \right)^{3/2}, \quad 0\%$$

$$\underline{\sigma(pp \rightarrow H + X) \times \text{Br}(H \rightarrow hh) \approx 20 \text{ fb}}$$

$$\Phi = \begin{bmatrix} \Phi^{0*} & \Phi^+ \\ \Phi^- & \Phi^0 \end{bmatrix}, \quad \langle \Phi \rangle = \frac{1}{\sqrt{2}} \begin{bmatrix} v & 0 \\ 0 & v \end{bmatrix}$$

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$$X = \begin{bmatrix} \delta^{0*} & \xi^+ & \delta^{++} \\ \delta^- & \xi^0 & \delta^+ \\ \delta^{--} & \xi^- & \delta^0 \end{bmatrix}, \quad \langle X \rangle = \frac{1}{\sqrt{2}} \begin{bmatrix} v_\Delta & 0 & 0 \\ 0 & v_\Delta & 0 \\ 0 & 0 & v_\Delta \end{bmatrix}$$

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Two singlets which mix to form mass eigenstates  $h$  and  $H$  are:

$$\begin{cases} H_1^0 &= \varphi, \\ H_2^0 &= \sqrt{\frac{2}{3}}\delta + \sqrt{\frac{1}{3}}\xi^0, \end{cases}$$

$h$  coupling constants:

$$\begin{aligned}\kappa_V &\approx 1 + 3 \left(\frac{v_\Delta}{v}\right)^2 \\ \kappa_f &\approx 1 - \left(\frac{v_\Delta}{v}\right)^2\end{aligned}$$

$$\mu \equiv \frac{\sigma}{\sigma_{SM}} \cdot \frac{\text{Br}}{\text{Br}_{SM}} = 1 + \mathcal{O}\left(\frac{v_\Delta^2}{v^2}\right)$$

$$\mu_{\tau\bar{\tau}} \approx 1 - \left(2\frac{v_\Delta}{v}\right)^2, \quad \mu_{VV} \approx 1 + \left(2\frac{v_\Delta}{v}\right)^2, \quad \mu_{b\bar{b}} \approx 1 + \left(\frac{2v_\Delta}{v}\right)^2.$$

The value  $v_\Delta = 50$  GeV is not excluded!

$$\sigma(pp \rightarrow H + X) \sim 2.5 \text{ pb}$$

$$\Gamma_{H \rightarrow hh} \approx \frac{v_\Delta^2}{v_\phi^4} \frac{3M_H^3}{16\pi} \left[ \frac{1 + 2 \left( \frac{M_h}{M_H} \right)^2}{1 - \left( \frac{M_h}{M_H} \right)^2} \right]^2 \sqrt{1 - 4 \frac{M_h^2}{M_H^2}}, \quad 98\%$$

$$\Gamma_{H \rightarrow ZZ} \approx \frac{v_\Delta^2}{v_\phi^4} \frac{M_H^3}{48\pi} \left[ \frac{1 - 4 \left( \frac{M_h}{M_H} \right)^2}{1 - \left( \frac{M_h}{M_H} \right)^2} \right]^2 \left( 1 - 4 \frac{M_Z^2}{M_H^2} + 12 \frac{M_Z^4}{M_H^4} \right) \sqrt{1 - 4 \frac{M_Z^2}{M_H^2}}, \quad 0.6\%$$

$$\Gamma_{H \rightarrow WW} \approx \frac{v_\Delta^2}{v_\phi^4} \frac{M_H^3}{24\pi} \left[ \frac{1 - 4 \left( \frac{M_h}{M_H} \right)^2}{1 - \left( \frac{M_h}{M_H} \right)^2} \right]^2 \left( 1 - 4 \frac{M_W^2}{M_H^2} + 12 \frac{M_W^4}{M_H^4} \right) \sqrt{1 - 4 \frac{M_W^2}{M_H^2}}. \quad 1.4\%$$

$\text{Br}(H \rightarrow hh) \approx 98\%$  for  $M_H = 300$  GeV,  
so direct searches in  $H \rightarrow ZZ$  mode do not lead to additional limits.

- Introduction of the isotriplet with hypercharge  $Y_\Delta = 2$  increases the  $2h$  cross section by the value which is comparable with that in SM.
- In the Georgi–Machacek model custodial symmetry is preserved so the limits on model parameters are much weaker and it is possible to significantly enhance the production of new scalar  $H$ .
- In the Georgi–Machacek model  $ZZ$  and  $WW$  decay modes can be very suppressed so  $H \rightarrow hh$  decays dominate.

Thank you!