Workshop on QFTHEP, Golitsyno, 08-15.September 2010

The problem of anomalous dilepton yield in relativistic heavy-ion collisions

A.A. Andrianov



Sankt-Petersburg State University



in collaboration with V.Andrianov, D. Espriu and X.Planells

Some highlights in: A. Andrianov, D. Espriu, P. Giacconi and R. Soldati, JHEP 09 (2009) 057 A. Andrianov, D. Espriu, F. Mescia and A. Renau, Phys.Lett. B684 (2010) 101

Tentative plan

- Dilepton production in central collisions in experiments on PHENIX (RHIC) ← NA60 (SPS) ← CERES (SPS) ← HADES (GSI) ← ← DLS (Berkeley) The first clear signs of an excess of dileptons above the known decay sources at SPS energies were obtained by CERES for M<1 GeV, NA38/NA50 for M>1 GeV and by HELIOS-3 for both mass regions . Years 1994-1995.
- 2. Cocktail of hadron decays into dileptons at high temperatures
 + dropping mass and /or broadening of meson resonances
 + enhancement of eta meson production in proton-neutron scattering
 = failure to explain abnormal dilepton yield
- 3. Large fluctuation of topological charge → chiral chemical potential in a fireball → "axion-like" background ~ condensate OR Spontaneous parity breaking due to pion condensate
 = time-dependent pseudoscalar background in collider kinematics
- 4. Parity breaking → splitting of masses for photon/vector meson polarizations → appearance of giant resonances
 → substantial enhancement of dilepton yield

Recent data from PHENIX RHIC



FIG. 27: (Color online) Invariant mass spectrum of $e^+e^$ pairs inclusive in p_T compared to expectations from the model of hadron decays for p + p and for different Au + Au centrality classes.

From: PHYS. REV. C 81, 034911 (2010) (PHENIX Collaboration)

TABLE IX: The enhancement factor, defined as the ratio between the measured yield and the expected yield for $0.15 < m_{ee} < 0.75 \text{ GeV}/c^2$, for different centrality bins. The meaning of the errors is defined in the text.

Centrality	Enhancement (\pm stat \pm syst \pm model)
00-10 %	$7.6 \pm 0.5 \pm 1.5 \pm 1.5$
10-20 %	$3.2 \pm 0.4 \pm 0.1 \pm 0.6$
20-40 %	$1.4 \pm 1.3 \pm 0.02 \pm 0.3$
40-60 %	$0.8 \pm 0.3 \pm 0.03 \pm 0.2$
60-92 %	$1.5 \pm 0.3 \pm 0.001 \pm 0.3$
Min. Bias	$4.7 \pm 0.4 \pm 1.5 \pm 0.9$

Central collisions

Small p_T → thermal sources of dileptons

Low masses = LMR, M_ee<1 GeV



This is an old puzzle!



Fig. 2. CERES experiment data collected in 2000 [17].

D. Miskowiec, Nucl. Phys. A 774, 43 (2006).





G. Agakichiev et al., Eur. Phys. J. C 41, 475 (2005).



Fig. 4. Distribution of pairs as a function of the transverse momentum in three ranges of masses [16].

G. Agakichiev et al., Eur. Phys. J. C 41, 475 (2005).

The oldest evidence of dilepton excess



HADES-experiment data on the dilepton yield

were obtained at the DLS setup (DiLepton Spectrometer) in the late 1980s. The setup was mounted at the accelerator Bevalac (Berkeley National Laboratory, USA). In the collisions between the ⁴⁰Ca + ⁴⁰Ca nuclei at $E_{lab} = 1.04$ GeV/nucleon.

R. J. Porter et al., Phys. Rev. Lett. 79, 1229 (1997)

Proton-neutron enhancement



Fig. 1. Invariant-mass spectrum of dielectrons detected in the (p, p) reaction.



Fig. 2. As in Fig. 1, but for the (d, p) reaction in the case where the quasifree neutron—proton channel is selected.

K. O. Lapidus Physics of Atomic Nuclei, 2010, Vol. 73, No. 6, pp. 985–987.

Not sufficient to saturate anomalous e+e- yield !

Hadron cocktail

Dilepton masses

Dominant Dalitz decays

< 140 MeV, < 550 MeV

 $\pi_0 \rightarrow \gamma e^+ e^-, \eta \rightarrow \gamma e^+ e^-$

Dilepton masses

300 MeV < M_ee < 900 MeV

Dominant 2-pion fusion

$\pi \tau$	$\tau \rightarrow$	ρ, ω	$\rightarrow \gamma^*$	\rightarrow	e^+e^-
~	-	-	• • • •		-

Hadron	direct	Dalitz	other
π^0	674	$\pi^0 \to \gamma \mathrm{e^+ e^-}$	
η^{0}	121	$\eta^0 \rightarrow \gamma \mathrm{e^+ e^-}$	$\eta^0 \rightarrow \pi^+ \pi^- e^+ e^-$
η'		$\eta' \rightarrow \gamma e^+ e^-$	$\eta' \rightarrow \pi^+ \pi^- e^+ e^-$
ρ^{0}	$\rho^0 \rightarrow e^+ e^-$	73	5
ω^0	$\omega^0 \rightarrow e^+e^-$	-	$\omega^0 \rightarrow \pi^0 \mathrm{e^+e^-}$
ϕ^0	$\phi^0 \rightarrow e^+ e^-$		$\phi^0 \rightarrow \eta \mathrm{e^+ e^-}$
J/ψ	$J/\psi \rightarrow e^+e^-$	$J/\psi \rightarrow \gamma \mathrm{e^+ e^-}$	50 61
ψ'	$\psi' \rightarrow e^+e^-$	$\psi' \rightarrow \gamma \mathrm{e^+ e^-}$	-
D mesons		ಗ	$D^{\pm} \to \mathrm{e}^{\pm} \nu_e + X$

TABLE I: List of decay channels relevant for dielectron production in p + p collisions at $\sqrt{s}=200$ GeV. For D^{\pm} mesons,



PHENIX: LMR anomaly



FIG. 42: (Color online) Invariant mass spectra of e^+e^- pairs in Au + Au collisions in the LMR. The data are compared to the sum of cocktail+charm (top left). The data are also compared to the sum of cocktail+charm and hadronic+partonic contributions from different models. The calculations are from The calculations are from (top right) Rapp and van Hees [15, 18, 83], (bottom right) Dusling and Zahed [19, 84, 85], and Cassing and Bratkovskaya [20, 27, 86, 87].

PHENIX: intermediate masses = IMR, 1<M<2.5 GeV



J.Manninen et al arXiv:1005.0500

FIG. 7: (Color online) Invariant mass spectrum of pairs of electrons and positrons in Au + Au (top) [2] and Cu + Cu(bottom) [54] collisions at $\sqrt{s}_{\rm NN}$ =200 GeV in different centrality classes compared with model calculations. The centrality bins are labelled from central to peripheral as 1 (0-10%), 2 (10-20%), 3 (20-40%). Centrality bin 4 consist on (40-94%) and (40-60%) most central events in Cu + Cu and Au + Au collisions, respectively, while the centrality bin 5 includes (60-92%) most central collisions. Both the data and

NA60 results on thermal dimuons



Fig. 9. Excess yield ratios for peak, continuum and total vs. centrality for the mass window 0.2 < M < 1 GeV. Open charm is subtracted throughout. No acceptance correction applied.

Photon(vector mesons) instability in pseudoscalar background

For slowly growing/decreasing neutral pion (isovector) condensate

$$\zeta \sim \alpha \langle \dot{\pi}_0 \rangle / \pi f_\pi$$

or large-scale isoscalar axion-like field

 $\zeta_{\mu} \simeq \delta_{\mu 0} \ \alpha \ \langle \dot{\theta}(t) \rangle / \pi f_{\pi} \simeq const$

$$\mu_5 = \partial_0 \theta / (2N_f)$$

← axial chemical potential

(in central heavy ion collisions)

Induced C-S term

$$\frac{1}{2}\varepsilon^{\mu\nu\rho\sigma}\,\zeta_{\mu}\,A_{\nu}(x)\,\partial_{\rho}\,A_{\sigma}(x)$$

Adiabatic approximation: in units $1/fm \sim f_{\pi}$

time derivative of CS vector << photon frequency/vector meson energy

P-and CP-odd condensates

Isoscalar condensate \rightarrow theta vacuum bubbles

D. Kharzeev, R. D. Pisarski and M. H. G. Tytgat, Phys. Rev. Lett. 81, 512 (1998)

K. Buckley, T. Fugleberg, and A. Zhitnitsky, Phys. Rev. Lett. 84 (2000) 4814

D. E. Kharzeev, L. D. McLerran and H. J. Warringa, Nucl. Phys. A 803, 227 (2008)

Isotriplet neutral condensate ="pion" condensate

A.A.Andrianov and D.Espriu, Phys.Lett. B 663 (2008) 450 (*and refs..therein*) A.A.Andrianov, V.A.Andrianov and D.Espriu, Phys.Lett. B 678 (2009) 416 (the talk by Vladimir Andrianov)

Start with

photons of different circular polarizations. They have different dispersion relation between their frequencies and wave vectors

$$\begin{array}{ll} \mbox{Polarizations} & A=T,L,+,-\\ \varepsilon_L^{\mu} = \frac{\zeta^{\mu}k^2 - k^{\mu}(\zeta \cdot k)}{\sqrt{k^2 \left((\zeta \cdot k)^2 - \zeta^2 k^2\right)}}; & \varepsilon_{\mu,L} \varepsilon_L^{\mu} = -1, & \mbox{Mass-shell} & k^2 = \mathbf{0} \end{array}$$

(Almost) circular polarizations of distorted photons

$$\varepsilon_{\pm}^{\mu}(k) \equiv \left[\frac{\mathbf{k}^2 - (\epsilon \cdot k)^2}{2\mathbf{k}^2}\right]^{-1/2} P_{\pm}^{\mu\nu} \epsilon_{\nu}$$

$$\hat{K}^{\mu}_{\nu}\varepsilon^{\nu}_{\pm} = \left(k^2 \pm \sqrt{(\zeta \cdot k)^2 - \zeta^2 k^2}\right)\varepsilon^{\mu}_{\pm}$$

Polarized decay !!

Time-like CS vector
$$(\zeta_{\mu}) = (\zeta, 0, 0, 0)$$
Mass-shell $k^2 = \pm \zeta |\vec{k}| \longrightarrow w_{\pm}(\vec{k}) = \sqrt{\vec{k}^2 \pm \zeta |\vec{k}|}$ Photon "-" is a tachyon $w_{\pm}(\vec{k}) = \sqrt{\vec{k}^2 \pm \zeta |\vec{k}|}$ Photon "+"decays
 $\gamma \rightarrow l^+ l^-$ with threshold $|\vec{k}| > 4m_e^2/\zeta$ Decay width is small $\Gamma_{\gamma} \simeq \alpha \zeta/3$

But the distorted photon is not a proper *Breit-Wigner* resonance as its position (effective mass) moves with momentum!

Threshold hierarchy!

If for electrons/positrons the threshold is of order 1 MeV then for muons it is four orders of magnitude higher , i.e. 10 GeV ! <u>No muon pairs excess in the PHENIX data!</u>? There is an excess in NA60!

Dilepton pair creation



| **k** | "On-shell" enhancement in a range of | k | ! $\sim \frac{1}{\Gamma_+\omega_+(|\vec{k}|)} \sim \frac{3}{\alpha M^2} \qquad |\vec{k}| \gg \frac{4m_e^2 - m_\gamma^2}{\zeta}, \zeta, n$

$$R_{enh}\Big|_{M\gg m_{\gamma}} = 3/\alpha^2 \sim 10^5$$

Taking into account thermal distribution

Boltzmann
$$f^B(k^0,T) = \frac{1}{e^{k^0/T} - 1}$$

For transversal polarizations

$$\frac{dN_{ee}}{dM} = M^3 \frac{\alpha^2}{9\pi^2} \int \frac{1}{[M^2 - m_{\rm eff}^2(|\vec{k}|)]^2 + \Gamma_{\pm}^2 w_{\pm}^2(|\vec{k}|)} \frac{\sqrt{(k^0)^2 - M^2}}{e^{k^0/T} - 1} dk^0 \qquad \qquad |\vec{k}| = \sqrt{(k^0)^2 - M^2}$$

Production rate is sensitive to temperatures via photon effective mass and width

RHIC temperatures T = 150 - 250 MeV

Photon thermal distribution makes resonances broader



Does it provide the abnormal ee excess in the range 100 – 700 MeV?

Only partially! Zeta scale is plausibly of order of few MeV's, $\zeta \sim \alpha f_{\pi} \sim 1 \text{ MeV}$ ρ, ω mesons must enter the game.

Finite-volume suppression (qualitatively)

A typical size of nuclear fireball $L \sim 5 \div 10 \text{ fm}$

Time spent by photons in nuclear medium $au_\eta \simeq L$

Resonance wave function and amplitude

$$\begin{split} \psi[\tau] &= \exp\left((-i\omega - \frac{1}{2}\Gamma)\tau\right) \implies D[E] = i\int_{0}^{\tau_{\eta}} d\tau \exp\left((i\Delta E - \frac{1}{2}\Gamma)\tau\right) \\ &= \frac{\exp\left((i\Delta E - \frac{1}{2}\Gamma)\tau_{\eta}\right) - 1}{\Delta E + \frac{1}{2}i\Gamma}, & \Delta E = E - \omega \end{split}$$

$$\begin{aligned} &\text{Breit-Wigner} & & & \\ \text{In the peak for } \Delta E = \vec{0} & \Gamma\tau_{\eta} \ll \vec{1} & D_{\eta}(0)/D(\vec{0}) \simeq \Gamma\tau_{\eta}/2 \ll 1 \end{aligned}$$

$$\begin{aligned} &\text{Absolute enhancement} & & & \\ & & \frac{\Gamma_{+}\tau_{\eta}}{2} \frac{2}{3\Gamma_{+}\omega_{+}(|\vec{k}|)} \sim \frac{\tau_{\eta}}{3|\vec{k}|} \sim \frac{\tau_{\eta}\eta}{3M^{2}}; & |\vec{k}| \gg \eta, m_{\gamma} \end{aligned}$$

$$\begin{aligned} &\text{Relative enhancement} & & \\ & & R_{enh,fin}\Big|_{M \gg m_{\gamma}} \sim \frac{\tau_{\eta}\eta}{2\alpha} \end{aligned}$$

$$\begin{aligned} &\text{For} & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\$$

Mixing with vector mesons

$$\begin{aligned} \mathcal{L}_{int} &= \bar{q} \gamma_{\mu} \hat{V}^{\mu} q; \quad \hat{V}_{\mu} \equiv -e A_{\mu} Q + \frac{1}{2} g_{\omega} \omega_{\mu} \mathbf{I} + g_{\rho} \rho_{\mu} \frac{\tau_3}{2}, \\ (V_{\mu,a}) \equiv (A_{\mu}, \, \omega_{\mu}, \, \rho_{\mu} \equiv (\rho_0)_{\mu}), \end{aligned}$$

$$Q = \frac{\tau_3}{2} + \frac{1}{6}; \qquad g_{\omega} \simeq g_{\rho} \equiv g \simeq 6$$
$$\mathcal{L}_{kin} = -\frac{1}{4} \left(F_{\mu\nu} F^{\mu\nu} + \omega_{\mu\nu} \omega^{\mu\nu} + \rho_{\mu\nu} \rho^{\mu\nu} \right) \qquad +\frac{1}{2} V_{\mu,a} (\hat{m}^2)_{a,b} V_b^{\mu};$$

$$\begin{split} (\hat{m}^2)_{a,b} &= m_V^2 \begin{pmatrix} \frac{10e^2}{9g^2} & -\frac{e}{3g} & -\frac{e}{g} \\ -\frac{e}{3g} & 1 & 0 \\ -\frac{e}{g} & 0 & 1 \end{pmatrix}, \text{ det } (\hat{m}^2) = 0, \\ m_V^2 &= m_\rho^2 = 2g_\rho^2 f_\pi^2 \simeq m_\omega^2 \end{split}$$

Chern-Simons "mass"

$$\mathcal{L}_{mixing}(k) \propto -\frac{1}{4} \varepsilon^{\mu\nu\rho\sigma} \operatorname{tr} \hat{\zeta}_{\mu} \hat{V}_{\nu}(x) \hat{V}_{\rho\sigma}(x)$$
$$= \frac{1}{2} \operatorname{tr} \hat{\zeta} \epsilon_{jkl} \hat{V}_{j} \partial_{k} \hat{V}_{l} = \frac{1}{2} \zeta \epsilon_{jkl} V_{j,a} N_{ab} \partial_{k} V_{l,b},$$

For isosinglet condensate

 $\zeta_{\mu} \simeq \delta_{\mu 0} \, \alpha \, \langle \dot{\theta}(t) \rangle / \pi f_{\pi} \simeq const$

$$(N_{ab}) \simeq \begin{pmatrix} 1 & -\frac{3g}{10e} & -\frac{9g}{10e} \\ -\frac{3g}{10e} & \frac{9g^2}{10e^2} & 0 \\ -\frac{9g}{10e} & 0 & \frac{9g^2}{10e^2} \end{pmatrix}; \quad \det(N) = 0,$$

For isotriplet condensate $\zeta \sim \alpha \langle \dot{\pi}_0 \rangle / \pi f_{\pi}$

$$(N_{ab}^{\pi}) \simeq \begin{pmatrix} 1 & -\frac{3g}{2e} & -\frac{g}{2e} \\ -\frac{3g}{2e} & 0 & \frac{3g^2}{2e^2} \\ -\frac{g}{2e} & \frac{3g^2}{2e^2} & 0 \end{pmatrix}; \quad \det(N^{\pi}) = 0,$$

Mass splitting for transversal polarizations

Mass shell

$$\begin{split} K^{\mu\nu}_{ab}V_{\nu,b} &= 0; \quad k^{\nu}V_{\nu,b} = 0; \\ \hat{K}^{\mu\nu} &\equiv g^{\mu\nu}(k^2\mathbf{I} - \hat{m}^2) - k^{\mu}k^{\nu}\mathbf{I} - i\varepsilon^{\mu\nu\rho\sigma}\,\hat{\zeta}_{\rho}k^{\sigma}\hat{N}, \end{split}$$

for transversal polarizations

$$\hat{K}^{\mu}_{\nu}\varepsilon^{\nu}_{\pm} = \left(k^{2}\mathbf{I} - \hat{m}^{2} \pm \sqrt{(\zeta \cdot k)^{2} - \zeta^{2}k^{2}} \; \hat{N}\right)\varepsilon^{\mu}_{\pm}$$

$$k_0^2 - \vec{k}^2 = m_V^2 \pm \frac{9g^2}{10e^2} \zeta |\vec{k}| \simeq m_V^2 \pm 360\zeta |\vec{k}| \equiv m_{V,\pm}^2$$

For massless photons and isoscalar condensate

$$N^{\theta} = \operatorname{diag}\left[0, \frac{9g^2}{10e^2}, \frac{9g^2}{10e^2} + 1\right]; \quad \hat{m}^2 = m_V^2 \operatorname{diag}\left[0, 1, 1 + \frac{10e^2}{9g^2}\right] \simeq \operatorname{diag}[0, 1, 1].$$

Transversal photon are not distorted and not decaying!

But for a mixture of isoscalar and isovector condensates they do decay.

$\pi\pi \rightarrow e^+e^-$ channel and VMD



Normal rho meson resonance for longitudinal polarization

"Giant" resonances for transversal polarizations with variable position

 e^+e^-

$$e^+e^-$$

$$\frac{dN_{ee}}{d^4xdM} \simeq c_V \frac{\alpha^2 \Gamma_V m_V^2}{3\pi^2 g^2 M^2}$$

$$\frac{dN_{ee}}{d^4xdM} \simeq c_V \frac{\alpha^2 \Gamma_V m_V^2}{3\pi^2 g^2 M^2}$$

$$\times \left(\frac{M^2 - n_V^2 m_\pi^2}{m_V^2 - n_V^2 m_\pi^2}\right)^{3/2} \Theta(M^2 - n_V^2 m_\pi^2)$$

$$\times \sum_{\epsilon} \int_M^{\infty} dk_0 \frac{\sqrt{k_0^2 - M^2}}{e^{k_0/T} - 1} \frac{m_{V,\epsilon}^4 \left(1 + \frac{\Gamma_V^2}{m_V^2}\right)}{\left(M^2 - m_{V,\epsilon}^2\right)^2 + m_{V,\epsilon}^4 \frac{\Gamma_V^2}{m_V^2}},$$

Dalitz decays

$$\pi_0 \to \gamma e^+ e^-, \eta \to \gamma e^+ e^-$$

low invariant masses < 300 MeV

$$\frac{d\Gamma_{\Pi \to \gamma ee}}{dM} \simeq \sum_{V} c_{\Pi} \frac{\alpha^3 m_{\Pi}^3}{48\pi^3 f_{\Pi}^2} \left(1 - \frac{M^2}{m_{\Pi}^2}\right)^3$$
$$\times \sum_{\epsilon} \int_{M}^{\infty} dk_0 \frac{\sqrt{k_0^2 - M^2}}{e^{k_0/T} - 1} \left|F(M, m_{V,\epsilon})\right|^2;$$
$$F(M, m_{V,\epsilon}) \equiv \left[\left(1 - \frac{M^2}{m_{V,\epsilon}^2}\right)^2 - i\frac{\Gamma_{Vee}}{m_V}\right]^{-1},$$

10)

$$m_{V,\epsilon}^2 \simeq M_{\rho}^2 + \epsilon \ 360 \ \zeta |\vec{k}|; \ m_V^2 \equiv m_{V,0}^2 \simeq M_{\rho}^2;$$

 $\Gamma_{\rho ee}/m_{\rho} \simeq 10^{-5}; \ \Gamma_{\omega ee}/m_{\omega} \simeq 0.8 \cdot 10^{-6}$



Abnormal enhancement of dilepton yield



The normalization of the $\rho+\omega$ peak is chosen on the PHENIX data

Compare with PHENIX



Signatures and searches of parity breaking

- Positions of resonances with two transversal polarizations depend on vector meson wave vector k and therefore convolution with thermal meson distribution makes them broader. Distorted vector meson resonances trigger considerably the yield of dileptons (see Fig. 1-3). Therefrom it follows that an empirical value of ζ ~ 1 – 2MeV.
- As the amplification of dilepton yield at a given value of their invariant mass is owed to photons/vector mesons with a definite polarization one could search for polarization asymmetry in event-by-event measurements. These measurements may reveal in an unambiguous way the existence of parity violation.
- For distorted photons with "+" polarization there are different thresholds ~ 4m_l²/ζ to start a resonant behavior for different dilepton species (five orders of magnitude between e⁺e⁻ and μ⁺μ⁻). For massive vector mesons such a difference in thresholds are smeared out and one could expect also an abnormal dimuon excess for invariant masses > 300MeV (presumably seen in [26]).
- Mixing with vector mesons is sensitive to isospin of pseudoscalar condensate and therefore the fraction of distorted photon decays helps to disentangle its isospin content.

<u>Program for</u> RHIC → CBM FAIR + NICA